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Research Article

Quantitative Feedback Control of Multiple Input Single Output Systems

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This paper presents a robust feedback control solution for systems with multiple manipulated inputs and a single measurable output. A structure of parallel controllers achieves robust stability and robust disturbance rejection. Each controller uses the least possible amount of feedback at each frequency. The controller design is carried out in the Quantitative Feedback Theory framework. The method pursues a smart load sharing along the frequency spectrum, where each branch must either collaborate in the control task or be inhibited at each frequency. This reduces useless fatigue and saturation risk of actuators. Different examples illustrate the ability to deal with complex control problems that current MISO methodologies cannot solve. Main control challenges arise due to the uncertainty of plant and disturbance models and when a fast-slow hierarchy of plants cannot be uniquely established.

1. Introduction

This paper deals with systems where multiple inputs are used to govern a single output. Although scientific literature refers to them with diverse names, here they will simply be called MISO systems. In some cases, each individual output is accessible, as in distributed energy generation systems [1], decentralised production systems [2], or unmanned fleets [3]. Usually, this leads to complex multiloop control structures [4]. However, a lot of engineering MISO systems lack physical individual outputs or sensors to measure them. Such systems are common in process industry [5], where the MISO control sometimes pursues the management of the global production system [6], whereas other times it governs low-level process variables (typical examples are two pumps or a pump and a valve, used as actuators in pressure or flow control [7–9]). In other cases the MISO control attends certain subsystems in a process, such as chemical reactors [10-12] or biological reactors [13-15]. More specific usages can be found in drying sections of paper machines [7, 16] or in aerobic digesters of waste water treatment plants [17]. Heat exchangers [18-20], chemical reactors in polymerization processes [9, 18], or distillation columns [9, 20-23] are repeated references in

the scientific literature as MISO control applications. The automotive industry has also adopted these principles, firstly for the government of internal combustion engines [24–27] and recently for HCCI (Homogeneous Charge Compression Ignition) engines [28–30]. Another area devoted to MISO control is the consumer electronics, and particularly the massive data storage devices [31–33]. And finally, biological engineering applications can be found in [18, 34].

Within those MISO systems with nonindividual measurable outputs, the control strategies can be divided into noncollaborative and collaborative ones. Noncollaborative control selects a plant inside a battery of them, which covers a wide range of operating points for the output. The selection criterion is based on the stationary capacity of each plant. Thus, the control law is designed for an equivalent SISO system. A selector splits online the control action to the plant or plants with capacity to regulate the output in the actual operating point. The *split-range control* [35, 36] is the most representative of this methodology. A simpler method reduces to a pure SISO control system, which closes a single feedback loop around a plant. The inputs to the other plants are manipulated manually or are left constant [37].

On the other hand, collaborative strategies benefit from the dynamic strengths of each plant to improve the controlled output performance considering the restrictions of manipulated variables and individual outputs. In the scientific literature collaborative MISO systems appear under diverse designations: VPC (*Valve Position Control*) [8, 9, 21–23], *habituating control* [10–12, 17, 18, 34, 38], *main-vernier control* [39–42], *cooperative-feedback control* [20, 43, 44], *load sharing control* [2, 45–47], or *PQ design method* [27, 48, 49]. *Midranging control* [7, 13, 15, 16, 35, 50–54] is frequently found in process control literature.

The controlled collaboration of parallel plants can be performed by serial (Figure 1(a)) or parallel (Figure 1(b)) structures of controllers. Serial collaboration is based on a qualitative organization of plants: the main loop $c_n p_n$ corresponds to the fastest plant p_n , the first one to react to output deviations. The vernier loops are arranged to produce a chained intervention of gradually slower plants. The last loop, which incorporates the slowest plant, is in charge of the steady state. In this way, each system collaborates to the extent it provides benefits, avoiding useless actuator fatigue and risk of saturation. This is also the goal of parallel structures. However, the involvement of each plant is determined by its preceding controller, instead of by its position in the overall scheme. Thus, the design of each openloop transfer function $c_m c_i p_i$ becomes more complex, since it has to define both the actuation domain and the action itself. However, unlike serial structures, parallel designs can cope with systems where the fast-slow hierarchy cannot be uniquely established.

In addition to all this, a proper design must pay some attention to the pervasive presence of uncertainty. In this sense, some solutions for the MISO control problem come from the Quantitative Feedback Theory (QFT). Horowitz [4, 55] did not pay much attention to the MISO problem with no individual measurable outputs. His work suggests the reduction of the MISO system to a SISO equivalent by plant summation. Then, a master controller $(c_m \text{ in Figure 1(b)})$ is designed for the equivalent plant, and no individual controller is used $(c_i = 1, i = 1, ..., n)$. The master control strategy can extract the maximum dynamic potential of each plant under certain restrictions for their phases. Nevertheless, its main drawback is that the same control action reaches all plant actuators. This entails using more feedback than necessary at certain frequencies on each branch, which leads to different negative effects in real-life actuators. In particular, an excess of noise amplification arises in the control actions to the slowest plants and steady-state offsets reduce the available actuation range for the fastest ones. Another drawback of plant summation strategy is that feedback is allocated by the plant instead of by the designer, losing some flexibility. This might have some importance in certain systems [7] whose high operation expenses suggest to arrange plant interventions according to monetary criteria rather than dynamic ones. Further QFT developments include the approaches in [25, 56], which detail a collaborative control of parallel plants with uncertainties and restrictions for particular applications, and the approach in [3], which adds feedback

loops of actuations inside a parallel structure as described in [57].

However, a general robust methodology to deal with MISO collaborative systems through QFT tools has not been presented yet. Such is the goal of this paper. In particular, it focuses on the disturbance rejection or regulation problem. The new technique is fitted to the parallel structure. This is the most versatile one since other arrangements can always be transformed into it while the inverse transformation is not always feasible. Besides, some examples will show that mainvernier design philosophy cannot cope with certain types of MISO plants. The new methodology seeks a quantitative division of feedback amongst parallel loops in the frequency domain. In absence of restrictions, this distribution leads to the accomplishment of the specifications with minimum use of feedback, that is, each loop only contributes at those frequencies where its plant favours the output performance.

2. MISO QFT Design Methodology

2.1. Robust MISO Regulation Problem. Consider Figure 1(b) with $c_m = 1$. Each parallel plant p_i , $i = 1, \ldots, n$, defines the effect of each manipulated variable u_i over the single measurable output y. The plant p_d defines the way in which the nonmeasurable disturbance d deviates the single output y from its desired constant set-point r. A set of parallel controllers c_i , $i = 1, \ldots, n$ are designed to minimize such deviation. Each c_i fixes its corresponding u_i based on a common output measurement y, which is corrupted by the noise signal n. For this regulation problem, the closed loop functions are

$$y = \frac{p_d}{1 + l_t} d - \frac{l_t}{1 + l_t} n,$$

$$y_i = -\frac{l_i p_d}{1 + l_t} d - \frac{l_i}{1 + l_t} n,$$

$$u_i = -\frac{c_i p_d}{1 + l_t} d - \frac{c_i}{1 + l_t} n,$$
(1)

where $l_i = p_i c_i$ are the individual open-loop transfer functions and

$$l_t = \sum_{i=1}^n l_i \tag{2}$$

is the global open-loop transfer function.

All plants are assumed to present parametric uncertainty. Let us define $\mathbf{q} = [q_1, q_2, \dots, q_m]$ as the vector of all parameters appearing in the transfer functions $p_1, p_2, \dots, p_n, p_d$. Each q_i varies within certain lower and upper limits. Therefore, the uncertainty vector \mathbf{q} belongs to a hyperrectangle in \mathbb{R}^m called the uncertainty space \mathcal{Q} ; that is,

$$\mathbf{q} \in \mathcal{Q} \triangleq \left\{ \mathbf{q} \in \mathbb{R}^m \mid q_i^- \le q_i \le q_i^+, i = 1, \dots, m \right\}.$$
 (3)

The purpose of QFT control is to enforce the specifications for all elements in the uncertainty space. In this case, the specifications include robust stability,

$$\left| \frac{l_t}{1 + l_t} \right| \le W_s \quad \forall \mathbf{q} \in \mathcal{Q}, \tag{4}$$

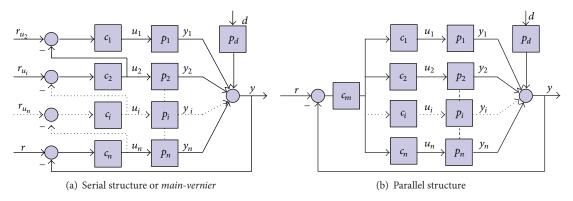


FIGURE 1: Control structures for MISO plant.

and robust disturbance rejection,

$$\left| \frac{p_d}{1+l_*} \right| \le W_d \quad \forall \mathbf{q} \in \mathcal{Q}, \tag{5}$$

where W_s and W_d are upper tolerances for each closed-loop frequency response.

As long as feedback control guarantees expected specifications at a certain price, QFT advocates for that control solution with the minimum amount of feedback, which will be denoted as the QFT optimum. In SISO control, the bounds express the minimal gain requirements on the nominal open-loop transfer function for the accomplishment of the specifications. Consequently, an QFT optimal loop-shaping tries first a narrow fulfilment of the bounds, and then an abrupt roll-off to minimize the presence of noise in the control signals [58].

In the MISO case, the search for the QFT optimum is not so obvious. There is a minimal gain of the nominal open-loop global function l_{t_o} that meets (4) and (5). However, it can be achieved by several combinations of l_{i_o} in (2). That combination of minimum gains of each c_i at each frequency is the solution that demands the minimum amount of feedback. Then, one option is splitting the global problem in several designs l_{i_o} in such a way that each bound arrangement shows the minimum amount of feedback solution. If so, each loopshaping reduces to a narrow fulfilment of the bounds and a maximal reduction of gain in the frequencies where no restrictions are imposed.

In practice, the new methodology looks for a wise distribution of feedback, which exploits the power of each plant frequency response to achieve controllers of minimum gain. This minimizes the presence of noise in the control signals to the slowest plants, which usually exhibit the most powerful actuators and provide the bias action. In this way, faster plant actuators preserve their full range of operation for output regulation in response to disturbances.

2.2. Parallel Plants and the Amount of Feedback. The core of the method is to quantify the amount of feedback, which is evaluated with the controller gain. For a better understanding, let us take a single frequency, exclude the uncertainty, and consider solely the specification of robust

disturbance rejection. Then, certain l_t will be a solution to (5). Two parallel structures from Figure 1(b) will be studied: a master control, which sintonizes c_m , and does each $c_i = 1$, and a strictly parallel control, which sintonizes each c_i and does $c_m = 1$.

To achieve l_t , we are firstly comparing the controller gain necessities for plants of similar characteristics. For simplification purposes, let us take two plants p. As expected, if the system power to regulate the output was increased from p to 2p, feedback necessities would reduce in the same proportion from $|l_t/p|$ to $|l_t/2p|$, independently if a master controller or two parallel controllers were used.

Secondly, control necessities to achieve l_t are being evaluated for plants with very different gains at the same phase. Let us take two plants as $|p_1| \gg |p_2|$. Note that, if p_1 plant worked alone, the feedback demand would be considerably inferior to the case of p_2 working alone: $|l_t/p_1| \ll |l_t/p_2|$. Therefore, there is no sense in using the p_2 actuation unless you consider other criteria different from meeting the performance with the minimum feedback. In the case of a master controller, its control demand is $|l_t/(p_1 + p_2)|$, which approaches to $|l_t/p_1|$. Thus, p_1 is the only plant contributing to the performance and p_2 actuator is being excited unnecessarily. A parallel controller structure can overcome this drawback as follows. Basing on the formulation, l_t = $c_1 p_1 + c_2 p_2$ can be achieved by different combinations of c_1, c_2 . However, as long as p_2 powerfulness is negligible, any attempt of collaboration with p_1 to the performance will require a huge control demand in the second branch. Then, the best option is to achieve the performance with the p_1 branch, whose control demand will be $|l_t/p_1|$. Simultaneously, tuning $c_2 \approx 0$ avoids that useless signals reach the p_2 actuators.

One of the above two situations (plants that should collaborate or not) arises in the loop-shaping of controllers at each frequency. In a first stage of the proposed methodology, special QFT bounds guide the designer to define when several plants are similar enough to collaborate at certain frequency or when they are different enough such that some must take the whole responsibility and others must be inhibited. Model uncertainty and the whole set of specifications are included in the method. In a second stage, the feedback is

shared accordingly through the sequential loop-shaping of controllers in the parallel structure.

- 2.3. First Stage: Load Sharing Planning at Each Frequency of Design. The proposed method firstly evaluates the amount of controller gain $|c_i|$ that each plant p_i would demand to fulfil the specifications (4), and (5) by itself, that is, assuming $c_{j\neq i}=0$. The required gain is expressed graphically by a QFT bound at each frequency ω , denoted by $\beta_{c_i}(\omega)$. Note that, unlike common QFT bounds, these are bounds on the controller gain, not on the nominal open-loop gain $|l_{i_o}|$, in the vertical axis. This is so, because their purpose is not to serve as design guidelines, but to allow a graphical comparison among the controller gains that are being demanded at subsequent design phase $\angle l_{i_o}$ by each plant. Once all the bounds for a single frequency ω are computed and a design phase Θ_d is selected for comparisons, a conclusion is reached according to the following criteria.
 - (a) If one of the bounds, say $\beta_{c_k}(\omega)$, is *sensibly* lower than the others at Θ_d , then regulation at that frequency must be accomplished through the openloop function l_k , and the other branches must be inhibited by decreasing the gain of $c_{i\neq k}(j\omega)$ as much as possible. The quantity of 20 log n dB is a practical guideline to establish the bound height difference. It is funded on the ideal collaboration of n equal plants, which would reduce n times the amount of feedback, as Section 2.2 details. Figure 2 shows the analysis for a 2-branch structure, which suggests that the controller c_2 should carry the burden of control at ω_1 whatever the chosen Θ_d is.
 - (b) If several bounds are located at the bottom and their heights do not differ too much from each other at Θ_d , then their associated controllers must share the regulating task. The branches whose bounds locate above this bound group must be inhibited. In this case, the practical rule of thumb is that any set of m bounds within a range of $\pm 20 \log m$ dB are suitable for cooperation. According to this, Figure 2 suggests that controllers c_1 and c_2 should collaborate at ω_2 whatever the chosen Θ_d is to fulfil the specification.

Remark 1. The first stage of the new methodology arranges the best load sharing amongst parallel plants at each frequency for minimum amount of feedback in each branch to meet the control specifications. This approach is completely new inside the MISO control literature.

2.4. Second Stage: Feedback Sharing in Parallel Structure of Controllers. Once it is decided which plants or plants must deal with the specifications at each frequency, the *n* parallel controllers are designed sequentially. The procedure presented here aims to minimize the number of iterations required to reach a feasible solution. At each step, one of the controllers is tuned by QFT loop-shaping, while the remaining ones are considered constant components of the overall uncertain system. This rotating nature of the tunable

controller is enabled by the *genbnds* command of the Terasoft QFT Toolbox [59], which admits general specifications in the form

$$\left| \frac{A + BG}{C + DG} \right| \le W. \tag{6}$$

Thus, if at some point the controller c_k is to be adjusted, the robust stability (4) bounds can be computed by choosing $A = \sum_{i \neq k} l_i$, $B = p_k$, $C = 1 + \sum_{i \neq k} l_i$, $D = p_k$, $G = c_k$, and $W = W_s$, while the robust disturbance rejection (5) bounds require the choice $A = p_d$, B = 0, $C = 1 + \sum_{i \neq k} l_i$, $D = p_k$, $G = c_k$, and $W = W_d$. Note that these are common QFT bounds, since they are imposed on the open-loop transfer function l_{k_o} , and consequently denoted $\beta_{l_k}(\omega)$, which represent all the specifications to meet at ω .

The design procedure begins with all controllers set to zero. Subsequently, in the first step of design, the loopshaping of the branch/branches that should work at the lowest frequency is performed fully. In an increasing order of frequencies, the last step corresponds with the design of branch/branches working at the highest frequency. During any loop-shaping design, the course of action at certain frequency depends on the result of the load sharing planning stage. As common in QFT for each loop-shaping, the design begins satisfying the bounds in an increasing order of frequencies, and finally, a fast roll-off of the open-loop gain is shaped in the high frequency range. A novelty of MISO control is that the open-loop gain must also be cut or reduced in the frequencies where the branch should be noncollaborating. Following, there are some hints of guide for both goals of design: when the branch must achieve the performance at ω and when the branch must be inhibited at ω because other branches do the work or because ω is the roll-off frequency for the branch.

At the frequencies where the branch/branches must perform the regulation task, two different cases are detailed next. Figures 3 and 4 show examples of both cases. Superscripts in bound designation indicate the step in the sequential design.

- (a) A single plant p_k will be responsible for the regulating task at ω (see the two-branch example in Figure 3). Thus, l_{k_o} is placed above the bound $\beta_{l_k}(\omega)$ (see l_{1_o} and $\beta_{l_1}^0$). After this, the k bound arrangement does not change (see $\beta_{l_1}^1$). However, since the accomplishment of the specifications has just been secured by c_k , the bounds $\beta_{l_{i+k}}(\omega)$ delimit now closed forbidden regions, which will allow a reduction of the $l_{i_o \neq k_o}$ gains for feedback saving at ω when these designs are faced (compare $\beta_{l_2}^1$ with $\beta_{l_2}^0$). Note also that, an excess of l_{k_o} gain to meet β_{l_k} would imply a major contraction of $\beta_{l_{i+k}}$ if this was necessary in the design of the other loops.
- (b) A group of m plants will share the control task at ω (see the four-branch example in Figure 4, where m=3). Their loop shaping is carried out jointly as follows. For convenience, let us denote the group $p_{k_1}, p_{k_2}, \ldots, p_{k_m}$. Let us assume as well that c_{k_1} is tuned first. The purpose of the designer is to place

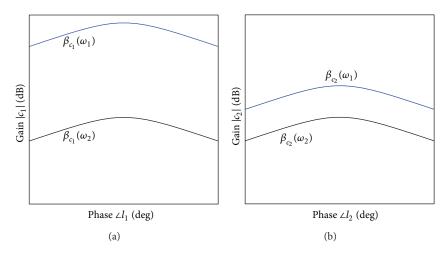


Figure 2: Feedback demand comparisons in a 2 \times 1 system.

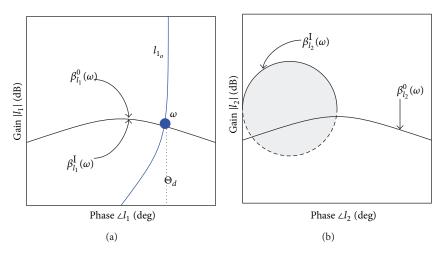


Figure 3: Single brach achieves the specifications at ω in a 2 \times 1 system.

 $l_{k_{1a}}$ around 20 log m decibels below the bound $\beta_{l_{k_{1}}}(\omega)$ at the design phase of interest Θ_d (see l_{1_0} and $\beta_{l_1}^0$). The consequences are that $\beta_{l_{k_1}}(\omega)$ bound does not change (see $\beta_{l_1}^{\mathrm{I}}$) and that a dip appears at Θ_d in bounds $\beta_{l_{k_j}}(\omega), j = 2, \dots, m$ (see $\beta_{l_2}^{\rm I}$ and $\beta_{l_3}^{\rm I}$). Then, tuning of $l_{k_{2a}}$ takes place, and the goal is to place $l_{k_{2a}}$ around $20 \log(m - j + 1)$, j = 2, decibels below the bound $\beta_{l_{k_2}}(\omega)$; (see l_{2_0} and $\beta_{l_2}^{\rm I}$). Once achieved, the $\beta_{l_{k_2}}(\omega)$ bound does not change (see $\beta_{l_2}^{II}$), but it extends the depth of the dip in $\beta_{l_{k_i}}(\omega)$, $j \neq 2$ (see $\beta_{l_1}^{II}$ and $\beta_{l_3}^{II}$). The process goes on in this manner, temporarily violating their bo-unds, until the tuning of $l_{k_{m_0}}$ is reached. In this case, the purpose is simply to meet the bound $\beta_{l_{k...}}(\omega)$, whose dip has been repeatedly enlarged by each one of the controllers c_j , j = 1,...,m-1 (see l_{3_o} and $\beta_{l_3}^{\mathrm{II}}$). Once this step is completed, all previously violated bounds are now met (see $\beta_{l_1}^{\text{III}}$, $\beta_{l_2}^{\text{III}}$, and $\beta_{l_3}^{\text{III}}$). If the m plants were identical at ω and Θ_d , the gain of each controller $c_{k_{1,\dots,m}}$ would be 20 $\log m$ dB lower. Nevertheless, differences between plant gains up to $\pm 20 \log m$ dB are acceptable for successful cooperation and controller gain reduction, as Section 2.3(b) reports. In consequence, some extra adjustments are usually necessary to meet each $\beta_{l_{k_j}}$. After the design of the m controllers with control responsibilities at ω , the bounds of the remaining loops will delimit closed forbidden regions (see $\beta_{l_i}^{\rm III}$).

At the frequencies where the branch/branches has/have no regulation responsibilities, a great deal of different situations may arise, specially when there are more than two inputs in the MISO system. Some of the most frequent ones are being described. In any case, the bound recalculation after any design step contributes to value the tradeoffs, which are inherent to any design with multiple degrees of freedom.

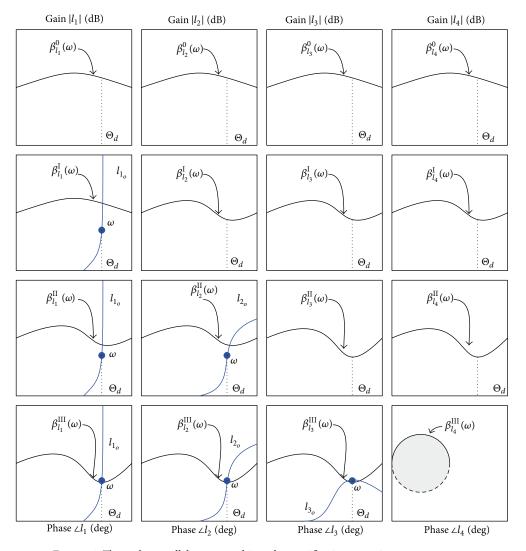


Figure 4: Three plants collaborate to achieve the specifications at $\,\omega\,$ in a 4 $\, imes\,$ 1 system.

- (i) Design hints for the roll-off frequencies ω of the k loop. The l_k gain reduction is usually a tradeoff between a maximum noise amplification and a minimum controller order. One case is that the bounds β_L demand certain feedback at ω . This happens if there are other loops with control responsibilities at ω that have not been designed yet. In this circumstance, the l_k design is performed temporarily violating its bounds at the roll-off frequencies ω . After the design of the loops with control responsibilities at ω , the bounds β_{l_k} are automatically reshaped and now demarcate forbidden closed regions. In the new picture, l_k will usually meet its bounds. Nevertheless, further iterations may be required to optimize the gain reduction at these roll-off frequencies. Other case is if the k loop is the last one to be designed. In this circumstance, $\beta_{l_{\iota}}$ bounds, which already delimit forbidden closed regions, are the definitive restrictions to be met in the l_{k_0} gain reduction at its roll-off frequencies.
- (ii) Design hints for the frequencies ω where the k plant participation must be inhibited. The bounds β_{l_k} currently demarcate fobidden closed regions at ω , since other loops have already achieved the prescribed specifications. The restrictions for the l_{k_o} gain reduction at frequencies ω are the bounds β_{l_k} at frequencies higher than ω , where the k plant will have to achieve or collaborate in the regulation task. The controller complexity is another reason to take into account in the gain saving procedure.

Remark 2. The second stage of quantitative MISO control details the QFT framework and procedure for the sequential loopshaping of parallel controllers in order to meet the predefined load-sharing arrangement. A set of branches collaborate in the control tasks or are inhibited for feedback saving. A standard method is given to deal with *n*-input single-output systems from a quantitative feedback control point of view, which remained unsolved till now.

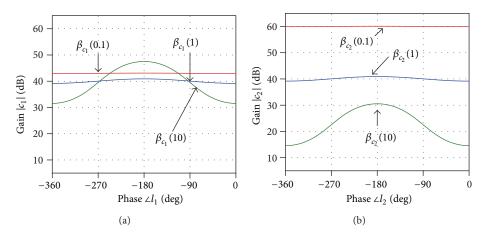


FIGURE 5: Feedback demands for single plant intervention.

3. Design Examples

3.1. Example 1. A simple MISO system illustrates the new methodology and its potential benefits. The uncertainty-free plant models are

$$p_1 = \frac{1}{10s+1}, \qquad p_2 = \frac{0.1}{0.1s+1}, \qquad p_d = 1.$$
 (7)

Inside a parallel disposition (Figure 1(b) with $c_m = 1$), the regulatory problem aims to design $c_{i=1,2}$ to meet certain stability (4) and performance (5) specifications with minimum controller gains at each frequency. For a minimum stability phase margin of 45°, the tolerance choice is

$$W_s = \left| \frac{0.5}{\cos(\pi (180 - PM)/360)} \right|, \qquad PM = 45. \quad (8)$$

And for disturbance rejection, the performance upper model is

$$W_d = \left| \frac{1.4167s (s+30)}{(s+10) (s+42.5)} \right|. \tag{9}$$

For bound computation and loop-shaping guide, a suitable vector of discrete frequencies is chosen:

$$\Omega = \{0.1, 0.5, 1, 5, 10, 100\} \left[\frac{\text{rad}}{\text{s}} \right].$$
 (10)

- 3.1.1. First Stage: Load Sharing Planning at Each Frequency. According to explanations in Section 2.3, the required amount of feedback at Ω is computed in case that a single system regulated the output: p_1 or p_2 , in Figure 5(a) and Figure 5(b), respectively (only three frequencies in Ω are drawn to illustrate the three potential outcomes). Compare controller bounds of both systems as follow.
 - (i) At low frequencies ($\omega < 0.5$), the bounds β_{c_1} ; see $\omega = 0.1$. Thus, p_1 branch should assume y regulation and p_2 branch should be switched off. Subsequent loop-shaping goals are $l_t \approx l_1$, $l_2 \approx 0$ at $\omega < 0.5$.

TABLE 1: Load-sharing planning for minimum amount of feedback.

ω	0.1	0.5	1	5	10	100
p_1	×	×	×			
p_2		×	×	×	×	×

- (ii) At medium frequencies (0.5 $\leq \omega < 2$), the bound heights differ less than 20 log 2; see $\omega = 1$. Thus, the collaboration of both plants is suggested. Subsequent loop-shaping goals are $l_1 \approx l_2$ at $0.5 \leq \omega < 2$.
- (iii) At high frequencies ($\omega \geq 2$), the bounds β_{c_2} are over 20 log 2 dB lower than the bounds β_{c_1} ; see $\omega = 10$. Subsequent loop-shaping goals are $l_t \approx l_2$, $l_1 \approx 0$ at $\omega \geq 2$.

Accordingly, Table 1 summarises the load sharing planning at design frequencies Ω .

- 3.1.2. Second Stage: Design of Parallel Controllers. Sequential loop-shaping of c_1 and c_2 is performed with Table 1 aims. Figure 6 illustrates the procedure in detailed steps. Steps 0, I, and II belong to the same first iteration, which explains the design of c_1 and c_2 (marked with superscripts). Further iterations (step III) are required to optimize both designs looking for the strictly minimum amount of feedback at each frequency, which usually trades off with a reasonable order of the controllers. General guidelines were described in Section 2.4.
 - (0) Initial bound computation is drawn with $c_2^0 = 0$ for the loop 1 (Figure 6(a)) and with $c_1^0 = 0$ for the loop 2 (Figure 6(b)).
 - (I) Loop-shaping of l_1 (see Figure 6(c)). To achieve $l_t \approx l_1$ at $\omega < 0.5$, l_1 is located onto bound $\beta_{l_1}(0.1)$. For plant collaboration at $0.5 \leq \omega < 2$, l_1 is shaped 20 log 2 dB below $\beta_{l_1}(0.5)$ and $\beta_{l_1}(1)$. At $\omega \geq 2$, the goal becomes $l_t \approx l_2$. Then, $\omega \geq 2$ are the roll-off frequencies for l_1 . Its gain is reduced as much as possible, even momentary violating bounds $\beta_{l_1}(5)$, $\beta_{l_1}(10)$, and $\beta_{l_1}(100)$,

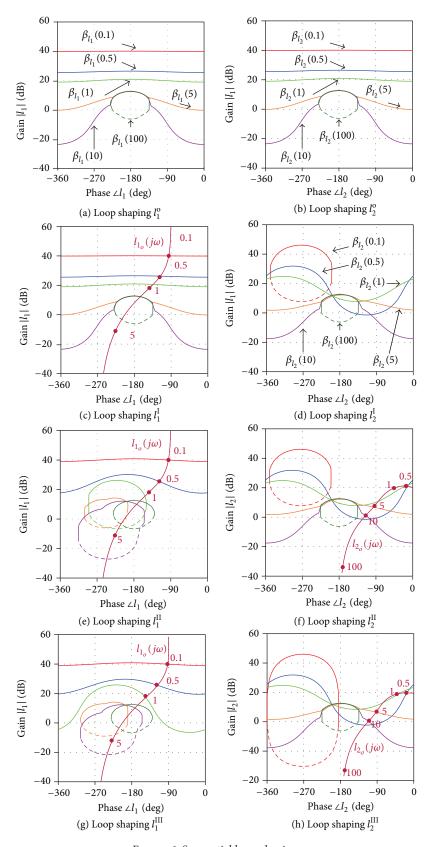


Figure 6: Sequential loop-shaping.

since control requirements will be achieved by l_2 . As this reduction is not bound guided, it could require later a l_1 reshaping at these high frequencies. After step I, the controllers are

$$c_1^{\rm I} = \frac{417(s+0.1)}{s(s+2)^2}, \qquad c_2^{\rm I} = c_2^0 = 0.$$
 (11)

As a consequence, suitable bounds β_{l_2} arise for the subsequent loop-shaping of l_2 . Let us compare new bounds in Figure 6(d) with initial bounds in Figure 6(b): closed exclusion regions appear in $\beta_{l_2}(0.1)$ for l_2 feedback saving at $\omega < 0.5$, since l_1 has already achieved the feedback requirements; dips arise in $\beta_{l_2}(0.5)$ and $\beta_{l_2}(1)$, where l_2 has to collaborate with previous l_1 contribution; the bounds at $\omega = \{5, 10, 100\}$ are not modified since l_2 must assume the whole control tasks.

(II) Loop-shaping of l_2 (see Figure 6(f)). Firstly, reduce l_2 gain at $\omega < 0.5$ to meet $|l_2| \ll |l_m|$, since $l_t \approx l_1$ was achieved. This example does not need adding a lag network, which favours a lower order of controller c_2 . Secondly, locate l_2 onto its bounds β_{l_2} at $\omega = \{0.5, 1, 5, 10\}$; note that the purpose of an excess of feedback at $\omega = 1$ is the illustration of subsequent optimization iterations. Finally, reduce the high frequency gain of l_2 at $\omega \geq 100$ (roll-off frequencies) as much as possible as in any *classical* QFT design. After step II, the controllers are

$$c_2^{\text{II}} = \frac{193.2 (s + 0.4) (s + 6.3)}{(s + 11) (s^2 + 1.2s + 0.51)}, \qquad c_1^{\text{II}} = c_1^{\text{I}}.$$
 (12)

As a consequence, let us compare new bounds β_{l_1} in Figure 6(e) with bounds of the previous step in Figure 6(c). Note that l_1 now meets all its bounds. Pay special attention to collaboration frequencies in Figures 6(e) and 6(f): the feedback sharing is close to the optimum at $\omega=0.5$ (l_1 and l_2 lie on their respective bounds), but it is not the case at $\omega=1$. Thus, small adjustments are required to economize feedback.

(III) Both loops are iteratively redesigned in Figures 6(g) and 6(h). Thanks to the help of software tools, this is usually a simple procedure. The final controllers are

$$c_1 = c_1^{\text{III}} = \frac{329.7 (s + 0.088)}{s (s + 1.5) (s + 2)},\tag{13}$$

$$c_2 = c_2^{\text{III}} = \frac{225.13(s+1.1)(s+6.95)}{(s+14.81)(s^2+1.77s+1.22)}.$$
 (14)

Note that l_1 achieves by itself the control requirements at $\omega=0.1$ and shares this task with l_2 at $\omega=\{0.5,1\}$. Thus, l_1 lies on β_{l_1} at $\omega=\{0.1,0.5,1\}$. Alongside, l_2 achieves by itself the performance load at $\omega=\{5,10\}$. Thus, l_2 lies on β_{l_2} at $\omega=\{0.5,1,5,10\}$. It's also necessary to remark how the bound disposition eases the reduction of the openloop gains, in particular at $\omega>1$ for l_1 and at $\omega<0.5$, $\omega>10$ for l_2 . Nevertheless, the feedback saving at these frequencies trades off with a minimum order of controllers.

3.1.3. Analysis and Comparisons. Parallel control, $c_{i=1,2}$ (13) and (14), is being compared with master control, c_m , which is designed for the equivalent plant $p_e = p_1 + p_2$ in order to satisfy the same performance and stability specifications. QFT design yields the single controller

$$c_m = \frac{192.6(s+0.1)(s+4.4)}{s(s+1)(s+8.9)}.$$
 (15)

For a fairer comparison, $l_m = c_m p_e$ lies exactly on its bounds and reduces its high frequency gain as much as possible. Thus, it is the solution of minimum amount of feedback at each frequency if the system was single input; Figure 7(a) depicts the minimum $|c_m|$. This QFT optimal loop-shaping is easily achievable as there is no uncertainty and there is a single controller. For the MISO solution, the exact meeting of bounds with controllers (13) and (14) required a second iteration to reshape the former controllers (11) and (12). Nevertheless, the main feedback saving is not so much to lie exactly on the bounds but to share conveniently the feedback between branches. Note that $|c_2| \ll$ $|c_m|$ at low frequencies, where p_1 regulates the output, and $|c_1| \ll |c_m|$ at high frequencies, where p_2 works. In this way, c_2 filters low frequencies, which avoids unnecessary offsets of p_2 actuation. And c_1 filters high frequencies, which reduces the amplification of high frequency signals (sensor noise) in p_1 actuator (usually labelled as cost of feedback in SISO QFT [58]).

Figure 8 clearly demonstrates these benefits in the time domain. External inputs are a unity step disturbance d(t)at t = 0.5 s and the sensor noise n(t) built with a whitenoise source (noise power = 0.001, sample time = 0.01). All response signals are depicted with and without noise intervention in blue and green lines, respectively. As long as $l_1 + l_2 \approx l_m$ (a better agreement could be achieved with higher order of controllers), the closed-loop transfer functions y/n and y/d are similar for both control strategies. Accordingly, the y(t) performance coincides for master and parallel control (only one is depicted in Figure 8), in presence (blue line) or absence (green line) of noise. However, the control effort strikes the differences as setting forward by closed-loop frequency responses in Figure 7(b). Let us compare the pair $u_1(t)$ - $u_2(t)$ with the signal $u_m(t)$ in Figure 8. Actuation $u_1(t)$ is hardly affected by sensor noise amplifications, which avoids unnecessary fatigue of p_1 actuator; the exact quantification of this benefit is on the distance

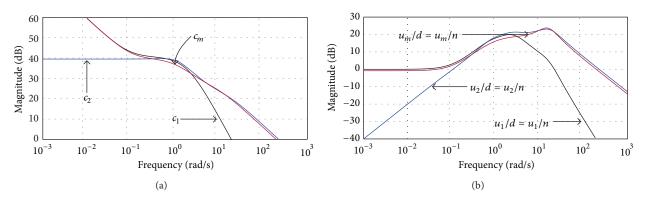


FIGURE 7: (a) Amount of feedback. (b) Closed-loop feedback cost.

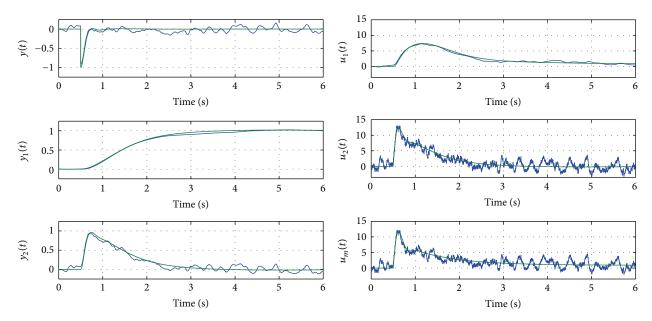


FIGURE 8: Time domain behaviour.

between $|u_1/n|$ and $|u_m/n|$, which mainly depends on the affordable bandwidth saving during the l_1 shaping. On the other hand, the noise n(t) affects similarly to both $u_2(t)$ and $u_m(t)$. However, $u_2(t)$ recovers the initial stationary state and $u_m(t)$ does not: see $u_2(t=\infty)\approx 0$, $u_m(t=\infty)=u_1(t=\infty)$ in time-domain, and $|u_2/d|_{\omega=0}\approx -\infty$, $|u_m/d|_{\omega=0}\approx |u_1/d|_{\omega=0}$ in the frequency domain. Thus, for accumulative disturbances, the fast time actuation of $u_2(t)$ starts out always from zero, and consequently, the full range of u_2 signal is available to speed up the transient response with a less saturation risk. Both improvements (the noise release of $u_1(t)$ and the zero steady state of $u_2(t)$) are more valuable in practice, where real-life plants, actuators, and sensors have physical limitations.

As some final comparisons, once c_1 and c_2 are achieved, there are equivalences in other MISO control topologies (Eitelberg's master-slaves [46] and Lurie's serial structure [39]) for this particular example. Designs according to those other structures and methodologies can always be transformed into the strictly parallel structure, while the inverse

transformation is not always feasible. In any case, the same QFT optimal solutions (13) and (14) would not probably be attainable since those other design methodologies do not quantify neither the amount of feedback nor the collaboration degree. Besides, some MISO plants or design-condition arrangements are only affordable with the new parallel design methodology; as following examples are discussing.

Remark 3. Firstly, this example details the two stages of the proposed MISO control methodology. Then analysis and comparisons show the expected benefits of a parallel structure of controllers in comparison with a single master controller: the reduction of useless fatigue and saturation risk of actuators. In comparison with other MISO control strategies (master-slaves or serial structures), the new one offers the minimum amount of feedback to govern each plant for prescribed specifications.

3.2. Example 2. Heat exchangers are common engineering applications of MISO control [18–20]. Figure 9 outlines

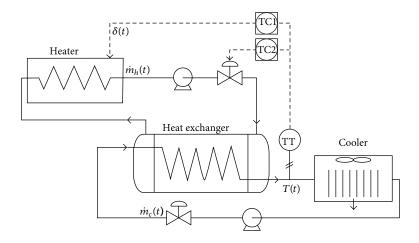


FIGURE 9: Thermal process control.

a heat-exchanger where the output temperature T(t), can be regulated through two manipulated variables: the hot flow $\dot{m}_h(t)$ and the heating power control $\delta(t)$ (which conditions the input temperature of the hot flow). The cold flow $\dot{m}_c(t)$ acts as a disturbance since the production rate changes on demand. A laboratory-scale plant commercialised by Feedback Systems Inc. agrees with this arrangement [60].

Around certain operating conditions, linear plant models of the form

$$p(s) = \frac{b_3 s^3 + b_2 s^2 + b_1 s + b_0}{s^4 + a_3 s^3 + a_2 s^2 + a_1 s + a_0}$$
(16)

are identified [61]. They express the relationships from the two manipulated variables to the output $(p_1 = T/\delta)$ and $p_2 = T/\dot{m}_h$) and from the disturbance to the output $(p_d = T/\dot{m}_c)$. A total amount of 112 cases are defined for each output/input relation, which generate the uncertainty of numerator and denominator coefficients in (16). Figure 10 depicts the envelopes of the plant frequency responses. As long as all the p-models are minimum phase, only magnitude Bode diagrams are included.

The robust stability control specification is (4) with tolerance (8) for a minimum phase margin of 45°. The specification for robust disturbance rejection is (5) with upper tolerance model

$$W_d = \left| \frac{1.2s(s+1.6)(s+5)}{(s+6)(s^2+1.6s+1.778)} \right|. \tag{17}$$

After computing the demand of feedback if p_1 or p_2 worked alone, Table 2 resumes the load-sharing planning at discrete frequencies to meet the robust control specifications with the minimum amount of feedback.

Consequently, the loop-shaping of l_{1_o} and l_{2_o} are performed (see Figure 11) and yield

$$c_1 = \frac{69.5 (s + 0.0044) (s + 0.058)}{s (s + 0.018) (s + 0.49) (s + 2.94)},$$
 (18)

$$c_2 = \frac{278.2(s+0.003)(s+0.052)(s+0.54)}{(s+0.0027)(s+0.016)(s+4)(s+20)}.$$
 (19)

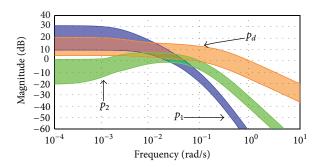


FIGURE 10: Frequency response magnitude plots of plants.

TABLE 2: Load-sharing planning along the frequency band.

Ω	0.005	0.02	0.05	0.2	0.5	1	10
p_1	×	×					
p_2		×	×	×	×	×	×

In Figure 12, closed-loop frequency responses illustrate the achievement of control specifications and the control effort that is used for it. Only the envelopes of a set of 112 frequency responses are depicted for each plant. In summary, the originality of this example relapses in the engineering character of the MISO plant, the robustness of the new methodology (model uncertainty consideration), and the challenge of disturbance incorporation through a dynamical model with uncertainty.

For comparison purposes, a master controller is firstly designed for the summation of plants $p_e = p_1 + p_2$ in order to meet the same robust control specifications

$$c_m = \frac{280 \left(s + 0.0044\right) \left(s + 0.058\right) \left(s + 0.38\right) \left(s + 0.58\right)}{s \left(s + 0.018\right) \left(s + 0.49\right) \left(s + 4\right) \left(s + 20\right)}.$$
 (20)

The parallel arrangement and the master controller behave equally attending to the prescribed stability and performance. However, the parallel one is superior in terms

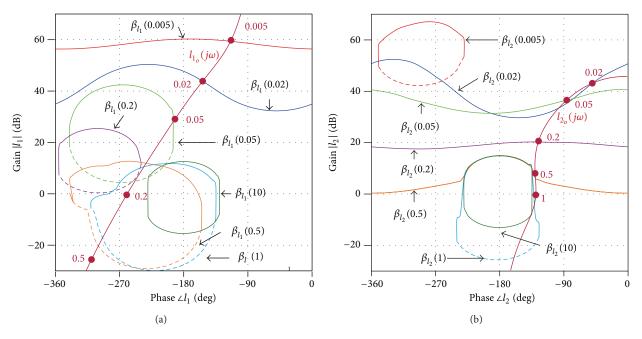


FIGURE 11: Loop-shaping of controllers.

of the actuation signals. The same reasoning and benefits of example 1 can be extended to this example.

Secondly, comparisons of the parallel arrangement and the master-slaves structures are shown. The master-slaves structure (Figure 1(b) with $c_m \neq 1$, $c_1 \neq 1$, and $c_2 \neq 1$) can be considered a particular case of the parallel structure (c_m = 1), since this last one will be demonstrated more versatile. Attending their functionality as filters, let us rename slave c_1 as filter f_1 and slave c_2 as filter f_2 . Let us suppose that c_1 (18) and c_2 (19) have already been designed for a parallel control structure. Then, there would not be a single equivalence for them in the master-slaves structure. Equivalents should meet: $c_m f_1 = c_1$ and $c_m f_2 = c_2$. A practical solution would be firstly to assume the master c_m of (20), as long as its output performance matches that of the set c_1 (18) and c_2 (19). And secondly, to overcome the drawbacks of master control for parallel plants, filters are computed as f_1 = c_1/c_m and $f_1 = c_1/c_m$ with c_1 (18) and c_2 (19). This equivalence procedure is also reliable in example 1. The inverse procedure, that is, the direct design of f_1 , f_2 , and c_m can be successfully done in example 1; however, it would become extremely difficult in example 2 for the following reasons. The master-slaves method firstly addresses the design of the filters and then the master. As a first difficulty, the filters have to perform the load sharing in frequency terms, but their manual open-loop design would not meet quantitative closed-loop criteria. Besides, the uncertainty in parallel plant models (p_1, p_2) hinders the choice of the cut-off frequency and the roll-off of the filters. Another difficulty is that the disturbance participation through dynamical models (p_d) makes impossible to guess the best load sharing along the frequencies between the parallel plants (p_1, p_2) , and then it hinders a suitable parametrization of filters. At a second step of the master-slave method of design, the master would be

designed, taking into account the initial MISO plant and the branch filters. In this stage, filter roll-offs may add serious problems: a high roll-off improves the filtering power but the branch phase deviates far from the original plant phase. Thus, branches can reach counter-phase conditions at certain frequencies. In such a case, a master controller spoils plant collaborations, since the vectorial sum $l_t = l_1 + l_2$ yields a smaller modulus than l_1 and l_2 .

Remark 4. A common engineering problem is solved: the robust regulation of output-flow temperature in a heat exchanger manipulating the input-flow heating power and the input heating flow itself, for different production rates (output-flows). Model uncertainty is fully considered to obtain the minimum amount of feedback controllers, whose benefits are detailed in previous examples. Additionally, the difficulties exhibited by the master-slaves strategy are overcome. The challenge is due to plant uncertainty and to the dynamical incorporation of disturbances.

3.3. Example 3. Despite the large number of engineering systems that have more than two manipulated inputs and single regulated output, few applications of this kind have been solved [40] so far. In fact, only a few scientific works incorporate a control theory for *n* inputs [25, 26, 45, 48, 56] because of its complexity. In this sense, the following example tries to demonstrate the potential of the new methodology. Consider a system with three manipulated inputs and a single regulated output, whose transfer function models are

$$p_i = \frac{k_i (a_i s + 1)}{(b_i s + 1) (c_i s + 1)}, \quad i = 1, 2, 3,$$
 (21)

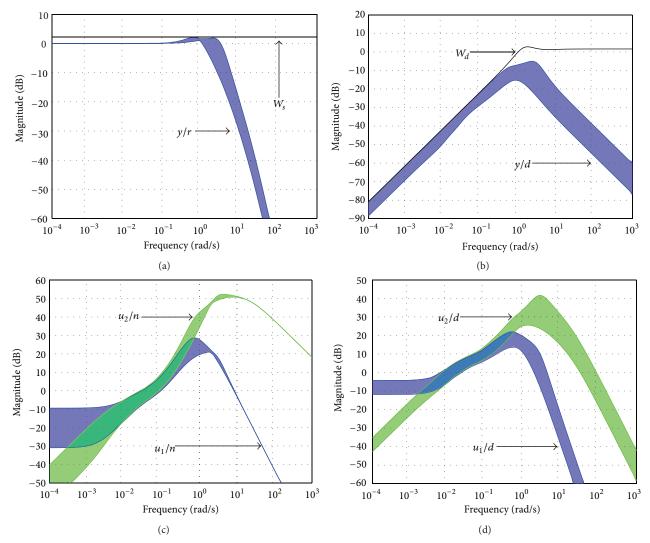


FIGURE 12: Closed-loop frequency response magnitude plots.

which are particularised for each i input by $k_1 = 100$, $k_2 = 10$, $k_3 = 1$, $a_1 = 10$, $a_2 = a_3 = 0$, $b_1 = 1000$, $b_2 = b_3 = 0.01$, and $c_1 = 0.1$, $c_2 = c_3 = 0$. Disturbances come into the single output straightforward, $p_d = 1$. As the difficulty of this example relapses on dealing with three actuators, parameter uncertainty has been intentionally omitted in the p_i plant models. Stability and disturbance rejection have to be attended meeting (4), (8) and (5), (9), respectively.

Upper section of Table 3 shows the amount of feedback $|c_i|$ that a single branch $c_i p_i$ would demand at the design phase $\Theta_d \approx -90^\circ$ to meet the specifications by itself. Note that the selection of design phase is part of the designer tasks. Previous examples depicted control necessities on the Nichols chart, that is, for all possible design phases $[-360^\circ,0^\circ]$. Consequently with the upper part, the bottom of Table 3 shows the planning on load sharing along the frequencies; revise the criteria in Section 2.3 to decide plant collaborations or not as a function of feedback demand $|c_i|$.

Accordingly to results and choices on Table 3, the loop-shaping of each l_i , i = 1, 2, 3 is sequentially performed

TABLE 3: (Up) Feedback demand; (down) load-sharing planning.

Ω	0.001	0.01	0.05	0.1	0.5	1	5	10	100
$ c_1 $	43	40	39	37	26	20	6	-3	20
$ c_2 $	60	40	27	23	20	20	19	13	40
$ c_3 $	80	60	46	40	26	20	5	-6	3
Ω	0.001	0.01	0.05	0.1	0.5	1	5	10	100
p_1	×	×			×	×	×	×	
p_2		×	×	×	×	×			
p_3					×	×	×	×	×

(see the final arrangements in Figure 13). The achieved controllers are

$$c_{1} = \frac{584.7(s + 0.0007)(s + 0.39)(s + 7.68)(s^{2} + 0.132s + 0.009)}{s(s + 0.0068)(s + 0.08)(s + 9)(s + 86)(s^{2} + 0.98s + 0.33)},$$
(22)

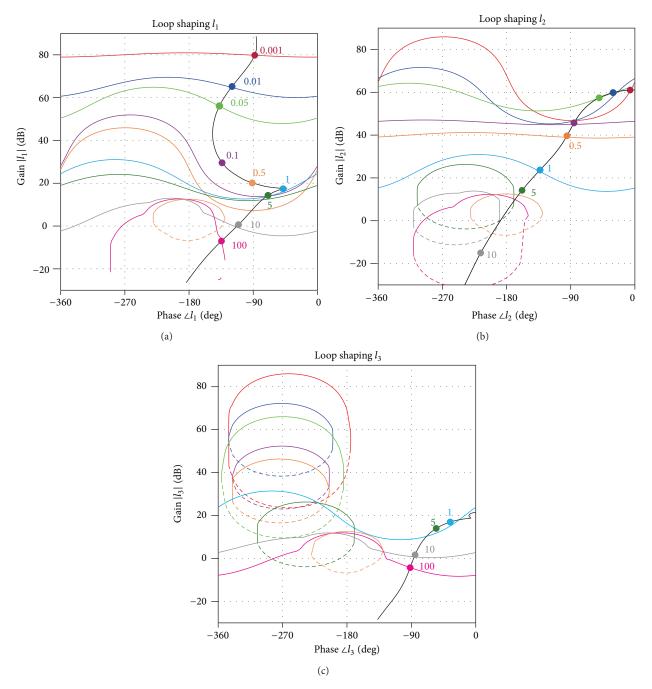


FIGURE 13: Loop-shaping of three parallel controllers.

$$c_2 = \frac{32.4 (s + 0.1)}{(s + 0.0087) (s + 0.63) (s + 5.27)},$$
 (23)

$$c_3 = \frac{6.155(s + 0.01)}{(s + 0.007355)(s + 0.7128)}. (24)$$

Figure 14 depicts the expected feedback sharing along the frequency band (Table 3) in terms of branch open-loop functions $|l_i|$ and their contribution to the global open-loop function $|l_t| = |l_1 + l_2 + l_3|$ in dB units.

The originality of this theoretical example relapses mainly in two challenges: facing regulatory problems with more than two manipulated inputs and dealing with parallel plants when some of them must work in disjoint bands of frequencies. Note that p_1 joins first at $\omega \in [0.001, 0.01]$ and later on at $\omega \in [0.5, 10]$. This causes that there is not an equivalent for c_1 (22), c_2 (23), and c_3 (24) in a serial structure (Figure 1(a)). Let us rename serial controllers as c_1^s , c_2^s , and c_3^s . The equivalents can be computed as $c_1^s = c_1$, and $c_2^s = -c_2/c_1$, $c_3^s = -c_3/c_2$, which would yield a nonproper controller c_3^s . On the other hand, it is not feasible either a straight away design of the serial controllers c_i^s using a main-vernier strategy, since the load sharing planning (Table 3) does not allow sorting the

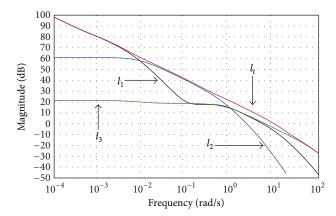


FIGURE 14: Open-loop responses on magnitude Bode diagram.

plants from faster to slower (p_1 joins at discontinuous intervals of frequencies). That is, the serial strategy is conceived for that each plant works in one and only one frequency interval.

Remark 5. This example tries to illustrate the new methodology ability (i) to solve regulatory problems of more than two manipulated inputs, which are frequent in engineering applications but are not so common in the scientific literature and (ii) to deal with parallel plants when some of them must work in disjoint bands of frequencies. For this last case, a serial structure of controllers (main-vernier) fails.

4. Conclusions

In attention to engineering application demands, a parallel structure of controllers has been proposed to solve MISO regulatory problems, which concern robust stability and robust disturbance rejection. MISO plant models included parametric uncertainty. Inside a QFT framework, a new methodology of design was proposed with the aim of tuning a set of controllers that met the robust specifications, and simultaneously, each controller used the least possible gain at each frequency. The keypoint was to quantify the feedback demanded by each plant at each frequency to meet the specifications by itself. This allowed a planning of the best load sharing along the frequency band. At each frequency, either one or several plants in collaboration must assume feedback responsibilities to meet the specifications or the plant/s participation must be inhibited for feedback saving. To accomplish it, a sequential design of the parallel controllers was fully detailed, using current QFT software tools for bound computations and for loop-shapings.

The abilities and engineering interest of the new methodology were demonstrated through several examples. The first one illustrated the methodology and detailed the benefits of a parallel structure of robust controllers in comparison with a single robust master controller. The main advantages are (i) to reduce the sensor noise amplification in the actuators of the slowest plants, which are conceived to work in the band of lower frequencies and provide the stationary and (ii) to avoid unnecessary offsets in the actuators of the faster plants,

and consequently, that their full range of actuation is available to speed up the response with less risk of saturation. Nevertheless, these are also the aims of current MISO methodologies, whose weak points have been also overcome by the new technique. In particular, a second engineering example exhibited the difficulties of tuning a parallel control using the master-slave philosophy. The challenge is mainly the filter (slaves) design due to plant uncertainties and the dynamic incorporation of disturbances, which are common in reallife plants. A third example illustrated the weak points of a chained serial structure of controllers (main-vernier), which fails when plants must work in disjoint bands of frequencies. In any case, the proposed parallel structure can always be converted to both master-slaves or main-vernier structures. The inverse procedure was demonstrated as not always being possible. In addition, the third example showed the difficulty of facing a MISO problem with three manipulabled variables, which are not common in the scientific literature but are frequent in engineering applications.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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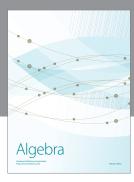
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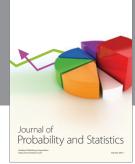
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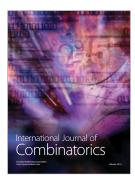














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