

Compact Dual-Band Terahertz Quarter-Wave Plate Metasurface

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Abstract—A dual-band quarter-wave plate based on a modified extraordinary transmission hole array is numerically analyzed and experimentally demonstrated at terahertz frequencies. To control independently orthogonal polarizations, the original square holes are connected with vertical slits and their lateral straight sides are replaced by meander lines. This smart design enables dual-band operation with unprecedented fractional bandwidths in a compact structure. Considering a flattening deviation lower than 40% of the optimum value, a fractional bandwidth of 53.8% and 3.8% is theoretically obtained (16.8% and 2.9% in the experiment) at 1 and 2.2 THz, respectively. At these two frequencies the structure is 0.13λ and 0.29λ thick, respectively. Given the compactness of the whole structure and the performance obtained, this quarter-wave plate is presented as a competitive device for the terahertz band.

Index Terms—Quarter-wave plate, terahertz applications, metasurface, extraordinary transmission, birefringence.

I. INTRODUCTION

During the last decades great efforts have been directed toward the development of terahertz (THz) technology due to the promising applications in imaging, semiconductor characterization and especially in biological and chemical sensing [1]. The development of THz (0.3-3 THz) time-domain spectroscopy has driven important advances in all these fields because it provides additional information to the widely used Fourier transform infrared spectroscopy [2]. This rapid progress has benefited from new generation and detection methods based on ultrafast pulses together with non-

linear crystals and photoconductive switches [3,4]. Further work can be found in the development of passive quasi-optical THz components such as lenses, filters or diffraction gratings [5,6]. Despite this activity, there is still a lack of efficient devices, especially those able to work wideband or multiband that benefit from the broadband feature of the above mentioned sources and detectors.

Among all these quasi-optical devices, polarizers are unquestionably of great interest. Classical polarizing devices exploit birefringent materials [7], whereby orthogonal polarizations encounter different indices of refraction. When the phase difference between orthogonal components of equal magnitude is 90 degrees, conversion from linear to circular polarized waves and vice versa can be achieved. This type of polarizers is called quarter-wave plate (QWP). At THz frequencies, QWPs based on photonic crystals made of quartz, calcite or even regular paper, have been proposed [8-10]. However, all these structures alike grating-based QWPs [11] are relatively thick (more than one wavelength at the operation frequency). This drawback can be overcome by means of metasurfaces, which can show form birefringence by properly adjusting the geometry of the unit cell [12-15]. Nevertheless, in most cases, their resonant nature leads to narrow bands which are insufficient in most applications.

In this work, we propose a very compact birefringent structure that works as a QWP at two different frequencies, 1 THz and 2.2 THz. At the highest frequency the proposed QWP operates at Fabry-Perot resonance, and thus, the fractional bandwidth is below 10%. However, at the lowest frequency, a large fractional bandwidth beyond those obtained with frequency selective surfaces (1.7 times larger) is achieved as a result of the off-resonance operation.

II. DESIGN AND EXPERIMENTAL PROCEDURE

As shown in the unit cell depicted in Fig. 1(a), the QWP proposed here is a modified extraordinary transmission hole array. The square holes composing the original array are connected with vertical slits and their lateral straight sides are substituted by meander lines. The structural parameters of the unit cell estimated from scanning electron microscopy (SEM) photographs are the following: $d_y=120\ \mu\text{m}$, $d_x=58\ \mu\text{m}$, slit width $w=4.9\ \mu\text{m}$, hole size $a_x=41.3\ \mu\text{m}$ and $a_y=47.9\ \mu\text{m}$, meander width $m=4.5\ \mu\text{m}$ and meander separation $s=7.475\ \mu\text{m}$. The metal pattern is gold (Au) with a thickness of $0.1\ \mu\text{m}$ and it is backed by a substrate of polypropylene (PP) of

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thickness $t=40\mu\text{m}$.

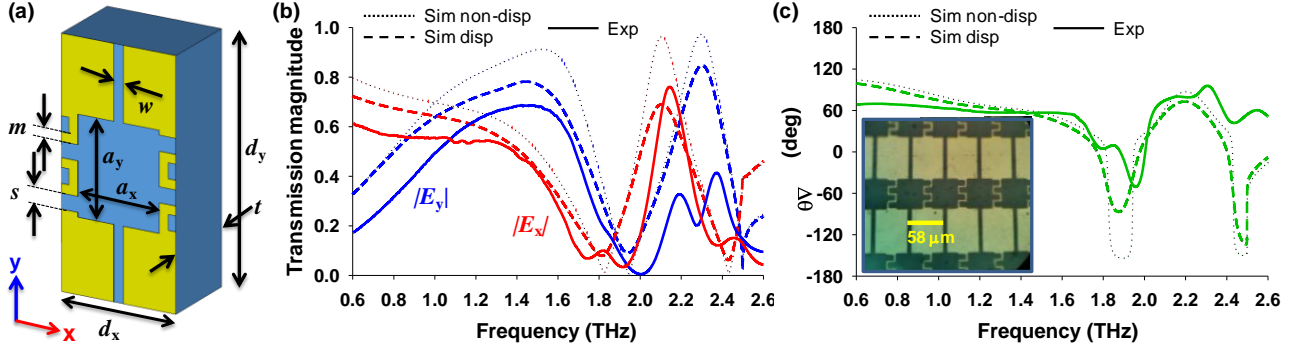


Fig. 1. (a) Unit cell. (b) Transmission magnitude and (c) phase difference between orthogonal components, when the structure is excited with a normal plane wave under x -polarization $|E_x|$ and y -polarization $|E_y|$. (inset) SEM photograph containing several periods of the prototype.

Two different approaches have been used in simulation to model the metal and the substrate. The initial optimization process of the structural parameters used a non-dispersive model where Au is assumed to have a finite electric conductivity equal to 4.561×10^7 S/m laying over a PP layer with a constant permittivity $\epsilon=2.22$ and loss tangent $\tan \delta=0.001$ [16]. Under these assumptions the device operates as an ideal QWP, see dotted lines in Fig. 1 (b,c). A parameter sensitivity analysis of this design is given in the supporting information. After the fabrication and measurement process, some deviation in the results was observed (see Section III for more details) and the previous simulation model was refined to explain the disagreements. A dispersive model was then used for both Au and PP: gold was modeled following a Drude model with plasma frequency $\omega_p=8.67 \times 10^{16}$ rad/s and collision frequency $\omega_c=6.64 \times 10^{14}$ rad/s [17]; and for the PP dispersive a complex permittivity is extracted from measurements of a pristine metal-free PP sample. Real and imaginary parts of the permittivity are within the ranges $\epsilon' \in \langle 2.21, 2.42 \rangle$ and $\epsilon'' \in \langle 0.1, 0.6 \rangle$, respectively. All simulation results have been obtained with the commercial software CST Microwave StudioTM using the frequency domain solver. The whole simulation is reduced to the analysis of a unit cell with Floquet boundary conditions under normal illumination. An adaptive tetrahedral mesh is set with a maximum step width of $0.3 \mu\text{m}$ on the metal.

A SEM photograph of the prototype can be seen in the inset of Fig. 1(c). The fabrication process is based on well-known “lift-off process”, widely used in silicon photonics, adapted here to work with flexible substrates. The process begins by fixing the PP film to a 6 inch silicon wafer. After this, a layer of Microposit S1813 photoresist is spin-coated in an EVG 101 coater tool, dried for a minute at 110°C in a hot-plate (TEL Developer Marz VZ) and exposed in an EVG 620 mask aligner. The metallization is performed in an e-beam evaporator physical vapour deposition system (Pfeiffer Vacuum Classic 500 tool). The final step consists on the lift-off of the remaining photoresist with the metal excess, leaving the metal structure on the PP substrate.

The experiment was performed using a TPS Spectra 3000

from Teraview under nitrogen purging condition [18]. A hundred single measures with a 6 GHz frequency step are taken to obtain an average representation of the transmittance. A plain sample of PP is used as reference.

III. RESULTS

The electromagnetic response of our wave-plate metasurface under normal incidence is fully determined from the analysis of two orthogonal polarizations parallel to the principal axes, x and y . Therefore, let us first study numerically the transmission properties of this metasurface for both orthogonal polarizations individually. The simulation results are plotted in Fig. 1(b,c) together with the experimental ones to facilitate the comparison. At low frequencies, under y -polarization (electric field parallel to the y -axis), transmission magnitude $|E_y|$ tends to zero while under x -polarization (electric field parallel to the x -axis), transmission $|E_x|$ tends to one (Fig. 1(b)). This is due to the aperture shape as it will be explained subsequently. In the non-dispersive case, both components cross at $f_0=1$ THz, when the transmission magnitude is equal to $|E_x(f_0)|=|E_y(f_0)|=1/\sqrt{2}$, i.e. transmittance is 50%. Moreover, a phase difference of $\Delta\theta(f_0)=85.3$ deg is obtained (Fig. 1(c)) with a negligible cross polar component (i.e. output E_x when the input is E_y and vice versa) of 0.03. Additional peaks rise for both components at 2.1 THz ($|E_x|$) and 2.3 THz ($|E_y|$) corresponding to a Fabry-Perot resonance between the metallic- and air-dielectric interfaces [19,20]. At $f_1=2.2$ THz, the transmission of both components is again equal $|E_x(f_1)|=|E_y(f_1)|=1/\sqrt{2}$, the phase difference is $\Delta\theta(f_1)=87.1$ deg and the cross polar component 0.02. Therefore, an almost ideal QWP is achieved in both bands.

Attending now to the experimental results, they clearly resemble the simulation ones. The number of peaks and dips accords with the simulation as well as the low frequency response. However, the high frequency peak for y -polarization is split into two probably due to fabrication imperfections which produce an undesired resonance. First and second band are centered at 1.07 THz and 2.29 THz, respectively in the measured structure. The magnitude of the transmission is

equal to 0.55 and 0.23, respectively, somewhat below the simulated values, suggesting that experimental losses are higher than expected. Notice that the QWP response is slightly blue-shifted, specifically 7% for f_0 and 4% for f_1 . Observing the phase difference, good agreement is also obtained over the whole frequency range. Major differences are observed around the dips at 1.9 THz and 2.5 THz, where the transmissions are zero and therefore fast phase changes might be expected [21] which are hardly measurable with the set up used. However, as they are located out of the bands of interest, they do not affect the performance. Specifically, at the center of the operation bands, a phase difference of 62.6 deg and 95.1 deg is measured for the lowest and the highest frequency, respectively.

Comparing the experimental results with the more realistic dispersive simulation, better agreement is obtained. Transmission values are closer because losses are better estimated and the frequency shift is partially predicted due to the dispersive nature of the model. Also the phase difference shows better prediction and the abrupt phase changes are softer, as they are in the experiment. A summary of the simulation and experimental results is shown in Table I where differences between simulation and experiment may be attributed to: (i) fabrication and material tolerances and (ii) misalignments during the experimental procedure (due to the flexibility of the structure, a flat and stable placement on the sample holder is difficult). The bandwidth (BW) is defined according to the flattening of the polarization state, as explained later.

TABLE I
SUMMARY OF THE QWP PERFORMANCE

	Sim. non-disp.	Sim. disp.	Exp.
f_0	1 THz	1.01 THz	1.07 THz
$ E_{xy} (f_0)$	0.7	0.64	0.55
$\Delta\theta(f_0)$	85.3 deg	74.2	62.6 deg
$BW(f_0)$	52.08 %	53.85%	16.77 %
f_1	2.2 THz	2.18	2.29 THz
$ E_{xy} (f_1)$	0.7	0.59	0.23
$\Delta\theta(f_1)$	87.1 deg	72.6 deg	95.3 deg
$BW(f_1)$	4.32 %	3.78%	2.90 %

The off-resonant and resonant feature of both bands is corroborated in Fig. 2 where the electric field under y -polarization is shown. It is observed at f_0 (Fig. 2(a)) how the electric field distribution shows a weak resonance condition in comparison with the field at the resonant frequency 1.5 THz (Fig. 2(b)), where it is mainly confined at the hole of the metallic layer. On the contrary, at f_1 (Fig. 2(c)), the electric field is extended to the whole substrate and the Fabry-Perot resonance is clearly noticed. Similar results are obtained for x -polarization where the field confinement in the aperture and the Fabry-Perot resonance are observed as well.

As shown, the precise combination of holes and slits yields in the desired magnitude and phase retardation between x - and y -polarization [22]. This can be easily explained from a

circuitual point of view. Under x -polarization, the electromagnetic wave effectively sees a modified slit array which behaves as a capacitance [23]. Hence the transmission tends to one at low frequency. On the other hand, under y -polarization, the wave sees essentially a modified hole array which is known to have an inductive behavior [24] and therefore, the transmission at low frequency tends to zero. This performance, based on complementary capacitive and inductive response, allows controlling the polarization state to achieve the desired 90 deg phase retardation between orthogonal components, as traditionally has been done, for instance, in classic meander-line polarizers [25]. However, the latter usually need a multilayer configuration to have high transmittance (at least two layers for similar performance).

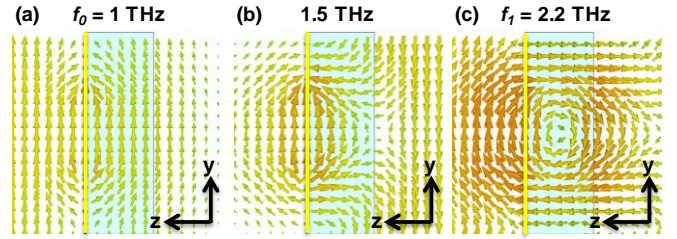


Fig. 2. Electric field representation on the yz -plane at the middle of the unit cell when the structure is excited with y -polarization.

Unlike a regular slit array, which shows a wide band response before the first order of diffraction (which is in fact our zone of interest), a regular hole array exhibits an extraordinary transmission resonance that it is narrow band by nature [26]. In order to achieve a wider band response, meander-lines are introduced between adjacent holes. It has already been proved numerically and experimentally [27, 28] that the total inductance and the bandwidth of the extraordinary transmission are increased with this technique. Notice that, in this work, the meander-line acts just as an inductance addition for the y -polarization, so it is not the source of the capacitance as in classical meander-line QWP [13, 25]. This capacitance is achieved for the x -polarization by means of the vertical slits.

In general, the electric field, at each propagation plane, is the superposition of the fields of both components, which in phasor notation is written as [19]:

$$\vec{E} = \hat{x}|E_x| + \hat{y}|E_y|e^{j\Delta\theta}. \quad (1)$$

which, assuming that the phase is deterministic, represents an elliptical polarized wave in the most general case

From here, it is straightforward to calculate the major semi-axis a and the minor semi-axis b of the polarization ellipse by simply taking $a = \max|\vec{E}|$ and $b = \min|\vec{E}|$. The polarization state can be quantified by the flattening parameter defined as:

$$flatt = 1 - (b/a) \quad (2)$$

which indicates the ellipticity of the polarization, where $0 \leq flatt \leq 1$, $flatt=0$ for circular polarization and $flatt=1$ for linear polarization. Considering $flatt < 0.4$ as an acceptable approximation to circular polarization, our design has a bandwidth of $BW(f_0)=0.47$ THz (16.77%) and $BW(f_1)=0.07$ THz (2.9%) in a structure as compact as $\lambda/7.5$ and $\lambda/3.4$ for

the 1 THz and 2.2 THz band, respectively. However, according to the simulation, a bandwidth around 50% and 4% might be achieved. In Fig. 3(a) it is shown the flattening for the whole frequency range. The measured flattening agrees well with the simulated one and it is observed how, where the bands are located, the flattening reaches the lower values. Around 1.9 THz a dip is observed in the dispersive simulation but its transmission magnitude is very low, see Fig. 1(b). Shaded areas indicate the bandwidths according to $flatt < 0.4$. The polarization state of the transmitted wave at the optimum frequencies (for the lowest flattening value) in each case is depicted in Fig. 3(b). Notice an acceptable experimental polarization state which is even better than the dispersive simulation at f_1 (although it is penalized by a lower amplitude transmittance) and the almost perfect circular shape for the ideal simulation.

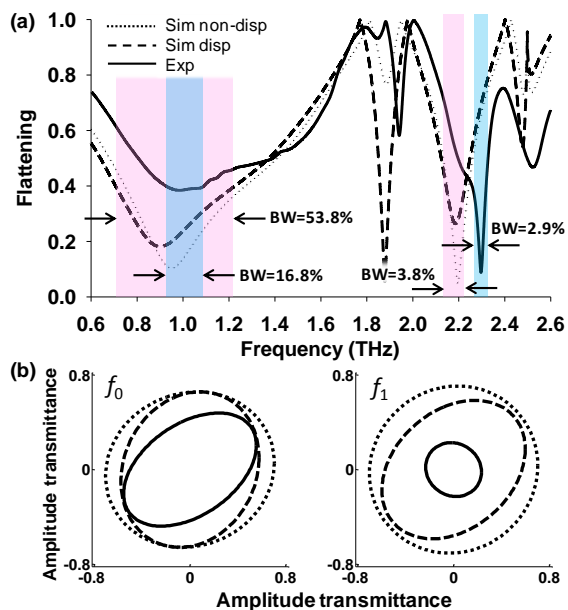


Fig. 3. (a) Flattening of the polarization state for the transmitted wave. Shaded areas represent the operational bandwidths. (b) Polarization state at the optimum frequencies.

IV. CONCLUSIONS

In conclusion, a very thin QWP working at two different bands in the terahertz-gap is presented. The form birefringence is achieved by means of the excitation of a complementary capacitive and inductive response which is obtained through a single layer extraordinary transmission modified hole array backed with a PP substrate. Wide and narrow operation bandwidths of 16.77% and 2.90% at 1.1 THz and 2.3 THz, respectively, are obtained after experimental results in a really thin structure of 0.29λ thickness. Numerical analysis also shows that better performance can be achieved up to fractional bandwidth of 53.85% and 3.78%. This work shows the potential that extraordinary transmission structures have for wave-plates competitive with those available in the literature (a comparison is given in the supporting information) and sets the bases for new THz quasi-optical polarizing devices.

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