Spatial-frequency multiplexing of high-sensitivity liquid level sensors based on multimode interference micro-fibers

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**ABSTRACT**

This paper shows a new fiber optic sensor multiplexed system for liquid level sensing. Biconical fiber tapers converging at a 40 mm-long micro-fiber are used as transducers. The tapers are designed to provide the propagation of the two main cylindrical modes in the micro-fiber avoiding higher order modes or modes with other symmetries. The liquid level is calculated in real time from the measurement of the frequency and phase components of the spectral interference pattern of the submerged micro-fiber. The system is fully characterized by theoretical simulations in terms of the sensitivity as a function of the most responsive parameter, which is the width of the micro-fiber. Phase sensitivities of 3.7 rad/mm are experimentally obtained and values as high as those of the micro-fiber 11.4 rad/mm are theoretically predicted. The strong dependence of the spatial frequency with the width of the micro-fiber has been used to multiplex three sensors in series in this domain. The maximum detected crosstalk between sensors is 0.2 rad/mm.

**1. Introduction**

Nowadays, liquid level sensing is indeed an active investigation field [1,2]. The need of precise level measurements of liquids mainly arises in industrial environments where large volumes of liquids are stored [3]. However, short and high-resolution level sensors are also required for minor containers in industrial areas such as medicine, biology [4] and even electronics manufacturing [5]. The market offers a wide variety of devices that base their functionality on many other technologies such as ultrasounds [6], capacitors [7], piezoelectric resonance [8], liquid resistance [9] or artificial vision [10]. Optical fiber sensors also join this list because many fiber configurations have been successfully proved for liquid level measurements. Among them, we find Mach-Zehnder interferometers [2,11], Sagnac loops [12], polymer optical fiber Bragg grating (POFBG) [13], or microstructured polymer optical fiber Bragg grating (mPOFBG) [14], D-shape fibers [15], no-core fibers [16], quasi-distributed fibers [17], multipoint pressure sensors [18] or codified fibers for digital applications [19] among others. Depending on the operating principle, these sensor systems show the following drawbacks. Power based sensors experience lower robustness and multiplexing difficulties. The presence of mechanical elements requires lubrication and maintenance of the sensor in order to minimize their deterioration over time. Complex fibers are expensive and difficult to find. Finally, sensors based on distributed measurements require high cost equipment.

Micro-fibers obtained from the biconical tapering of standard single-mode fibers (SMF) are structures widely used as sensors from long time ago [20,21]. Current technology allows the accurate and repetitive fabrication of intermediate long micro-fibers between biconical tapers making such structures suitable for short-range liquid level measurements. Heating and rapidly stretching the fiber, its nominal diameter can be narrowed down to a microwire of a few micrometers receiving the name of down-tapers [2]. Those tapered fiber sensors can be used either in a cascade configuration [22,23] or individually, as we do in this work. Likewise, waist diameter can be enlarged in an up-taper configuration [2], achieving also high sensitivity in liquid level measurement setups [24].

Micro-fibers are strongly confined cylindrical multimode structures defined by the silica waist and the surrounding medium. The incoming taper, properly designed beyond the adiabatic criterion, provides the excitation of higher order modes in the micro-fiber. The interaction of the modes along the propagation in the fiber provides an interference pattern in the optical spectrum [25]. The Fast Fourier Transform (FFT) of these fringes is calculated in real time [26] in order to obtain their spatial frequency and phase, both parameters being used to calculate the level of the liquid.

In this paper, we present the spatial frequency multiplexing of a system of highly sensitive tapered micro-fibers for different liquid level measurements. Preliminary results were published in OFS 26 [27]. The theoretical design process and simulation calculations are in good agreement with the obtained experimental results, and are also shown in this work.
The sensing transducers are based on biconical optical fiber tapered (OFTs) (see Fig. 1). We fabricated the tapers using standard communication single-mode fibers that were narrowed from its nominal diameter of 125 μm down to a micro-wire of several micrometers wide and 40 mm long. A Taper Manufacturing Station (TMS, 3SAE from NorthLab Photonics) was employed to fabricate the OFTs. This fiber tapering system operates in partial vacuum which is advantageous providing low loss and great repeatability [28]. The tolerance results are mainly dictated by fiber preparation rather than the TMS performance. The scanned waist diameters of a 125 μm fiber tapered to 62.5 or 25 μm could vary up to ± 1 μm or ~2%. In addition to this, if offers an automatic and built in taper scan function, that allows a real time check of the manufactured optical fiber taper.

Despite the reduced waist diameter of the fabricated OFTs, the micro-fiber holds tens of guided modes even for a diameter as low as 10 μm due to the high index contrast of the silica-air interface.

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**Table 1**

Propagation constants and related beating lengths for the two main modes HE_{11}, HE_{12} in the micro-fiber for three different diameters and for two different external substances: air and methanol.

<table>
<thead>
<tr>
<th>Width (μm)</th>
<th>HE_{11}</th>
<th>HE_{12}</th>
<th>HE_{11}</th>
<th>HE_{12}</th>
<th>HE_{11}</th>
<th>HE_{12}</th>
<th>Air</th>
<th>Methanol</th>
<th>L_{b-air}/L_{b-methanol}</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>63</td>
<td>33</td>
<td>5.918</td>
<td>5.796</td>
<td>5.920</td>
<td>5.810</td>
<td>51.7</td>
<td>57.0</td>
<td>0.91</td>
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<tr>
<td>15</td>
<td>64</td>
<td>31</td>
<td>5.935</td>
<td>5.890</td>
<td>5.936</td>
<td>5.893</td>
<td>137.7</td>
<td>145.7</td>
<td>0.94</td>
</tr>
<tr>
<td>20</td>
<td>67</td>
<td>30</td>
<td>5.940</td>
<td>5.816</td>
<td>5.940</td>
<td>5.917</td>
<td>260.5</td>
<td>271.2</td>
<td>0.96</td>
</tr>
</tbody>
</table>
Higher order modes extend deeper in the surrounding medium enhancing their sensitivity to refractive index changes in the environment as a result of the immersion of the micro-fiber in liquid.

The guided mode in the incoming SMF entering the first transition progressively transforms into the main guided mode of the micro-fiber. A smooth narrowing of the fiber longer than about 1 cm supposes an adiabatic transition where all the optical power remains in the fundamental mode of the waist. In such case, there would not be environment dependent intermodal interference. Therefore, a sharper tapering beyond adiabaticity has to be defined to the input taper in order to transfer optical power form the fundamental mode (HE$_{11}$) to the radially symmetrical second order mode (HE$_{21}$) minimizing the excitation of higher order modes. In this way, we obtain a clear interference pattern with a large amplitude when the micro-fiber is immersed in liquid.

A commercial fully vectorial finite difference mode solver [29] has been used for the analysis of the tapered fiber. The taper shape that better fits the transitions obtained by the fabrication station is a cosine interpolation function. Fig. 2 shows the mode power transmission as a function of the transition length for a minimum waist diameter of 10 μm. As expected in a symmetrically conical transition, radially symmetrical modes gather the optical power delivered by the fundamental mode if the adiabaticity criterion is broken down. The insets of Fig. 2 also show the intensity profiles of modes HE$_{11}$, HE$_{12}$ and HE$_{13}$. We confirm that the fundamental mode gradually losses power as the taper shortens and that this power efficiently transfers to the mode HE$_{12}$. For a compromise length of 2500 μm, the mode HE$_{12}$ reaches a 33% of the optical power whereas the mode HE$_{11}$ keeps a 63%. This distribution provides an adequate amplitude in the interference pattern. The rest of the cladding modes receive less than a 4% avoiding higher frequency interferences in the measurement that would also cause crosstalk in the multiplexed scheme. Wider diameters of the central waist show slightly lower power transfer to the HE$_{12}$ mode. A diameter of 20 μm ends up with 30% of the input power in the HE$_{12}$ mode in the micro-fiber.

Once the two main modes in the micro-fiber are excited, they experiment a periodic interference during propagation. Due to the reduced diameter of the waist, there is a considerable influence of the external material on the propagation and the interference of these modes. Table 1 shows the propagation constants of modes HE$_{11}$ and HE$_{12}$ for three different diameters and for two different external substances used in the level measurement tests (air and methanol). Corresponding modal power distribution induced by the tapered fiber and the beat lengths of the bimodal interferences are also shown. We see that the interference length of the main modes decreases substantially for smaller fiber diameters, but that the relative difference between beat lengths in air and liquid increases, which implies higher spatial frequencies and sensitivity.
3. Fabrication and experimental setup

The biconical non-adiabatic tapered fibers and the 40 mm-long microfibers were fabricated by heating the SMF with a thermally stabilized plasma in partial vacuum and applying a precise tension on both sides of the fiber. A microscopic vision system monitors the evolution of the width of the structure. This scheme results in a high quality, low loss and good repeatability tapering procedure [30].

Fig. 3 illustrates the experimental set up for the liquid level sensitivity tests. The tank was filled with methanol (NCAS: 67–56-1) for the immersion tests. The refractive index of the liquid is 1.3172 at 1.55 μm [31]. Two fiber optic Bragg gratings (FBG) were glued to both sides of the wall of the container for temperature evaluation. The C-shaped element holding the micro-fiber was made with glass in order to minimize the influence of the thermal expansion. The ends of the biconical tapered fibers were pre-strained using a 20 g load before gluing to the support to avoid undesired non-linear responses during tests. The linear actuator precisely governs the immersion depth, as well as its speed.

The measurement of the immersion depth of the tapered micro-fiber is based on the frequency and phase changes of the transmission interference pattern as a function of the liquid level. We obtain the fringes of the sensor in the optical spectrum using a commercial optical interrogator, Micronoptics Si155 [32] that offers a wavelength resolution of 10 pm and a wavelength accuracy of 1 pm for a 100 nm range. Then, we perform a real time calculation of the FFT of this spectrum and track the spatial frequency and phase of the main spectral component to obtain precise information of the measured parameter. The use of the FFT phase-based demodulation instead of conventional techniques (such as monitoring a peak/valley of the spectrum) allows achieving a higher effective resolution [33].

In this setup, channels one and two of the interrogator measure the transmission response of the sensor, whereas channel three quantifies the reflected wavelengths from the FBGs for temperature sensing. If necessary, these FBGs could be connected to the same fiber channel of the level sensor in a simpler scheme.

4. Results and discussion

Fig. 4 shows the measured optical transfer function in air of the microfibers for three diameter waists of 10, 15 and 20 μm. The patterns reveal a clean and regular interference suggesting an effective power transference from the main mode to the second order cylindrical mode. Power leakage to higher order modes in the tapered fiber would imply irregular and noisy fringes in the optical spectrum. The amplitude of the obtained signals ranges between 4 and 8 dB, slightly lower than the calculated values but still confirming a significant accumulation of optical power by mode HE_{12} (see also Table 1).
Smaller diameters mean bigger differences in the propagation constants between modes that at the same time imply shorter beat lengths. Therefore, the biconical tapered fiber is more sensitive to optical wavelength variations, showing higher interference frequencies in the pattern. These spectral frequencies, which are thoroughly tuned by the width of the micro-fiber, is the basis to multiplex several sensors into the same optical channel of the interrogator, as it is shown in the last section of this work. The normalized magnitude of the FFT of each interference pattern is shown in Fig. 5. The spatial frequencies of the main spectral components are $0.47, 0.18$ and $0.10 \text{ nm}^{-1}$.

Interferometric sensors are generally limited to relative measurements. The measuring process is phase-based, and measurements are referred to an initial position from which we track accumulative variations in successive periods [12]. In order to avoid this limitation, we trace the absolute position of the peak in the spatial frequency spectrum together with its phase as the micro-fiber immerses in liquid. Fig. 6 shows the normalized spatial frequency (SF) and phase evolution of the peak of each sensor as a function of the immersion depth. Note that a simple interpolation has been used in the calculation of the peak position for the ease of the spatial-frequency variation.

As expected, slimmer diameters experience larger variations in both parameters. We remark the excellent linearity of the frequency measuring confirming its potential to analyze this kind of sensors. Measured values adequately fit results predicted by simulations, except for the phase progression of the smaller waist where theoreti-
cal calculations show a much higher sensitivity than measurements: 11.4 versus 3.7 rad/mm. The technical issue shown up next clarifies this mismatch. The predicted sensitivity implies that we get an advancement of $2\pi$ radians in the phase for a displacement of only 0.55 mm in the immersion depth. Since the step of the linear actuator during the measurement was 0.4 mm, we are registering aliased information from a periodic signal. Therefore, we are not retrieving real information due to the huge sensitivity of the smaller micro-fiber.
Writing down the measured and calculated sensitivity values of the SF and phase as a function of the considered three diameters, we obtain the graph shown in Fig. 7. The aliased phase measurement for 10 μm has been removed. The phase sensitivity oscillates between 11.4 rad/mm (theoretical calculation) for the thinner fiber and 0.97 rad/mm for the widest; whereas the SF varies between 3 and 0.23 pm/μm/mm, respectively. The multiplexing of sensors over different spatial frequencies fabricating them with so many other diameters implies having diverse sensitivities for each one of them varying in the range of one order of magnitude.

In order to evaluate the behavior of the micro-fibers under temperature variations, we have tested newly fabricated specimens in a climatic chamber [34]. Inducing a temperature alteration of 20 °C, we have registered the evolution in the SF and phase of each sensor. The recorded temperature sensitivity is much lower than the variation induced by the immersion depth. In the worst case, which corresponds to one with 20 μm width, a temperature variation slightly higher than 20 °C is needed to generate an uncertainty of 1 mm in the liquid level value. Fig. 8 shows the phase displacement results for temperature variations for the three micro-fiber diameters.

Regarding the error of the measurements, the mechanical setup is the main error source. Both the linear actuator inaccuracy and the C-shaped support for the taper without a proper packing, make vibrations an important source of mismatch between measured and real values. Upgrades in the mechanical setup and a proper sensor packaging would improve the results. Compared to the error induced by the mechanical setup itself, other errors induced in the fabrication process or by the optical interrogator, can be considered negligible (after an adequate calibration of the sensor sensitivity).

5. Sensor multiplexing

In order to examine and validate a multiplexed sensor system based on the division of the SF of the optical spectrum, we fabricated three new biconical tapers and micro-fibers: S1, S2 and S3. Respective values of 17, 14.5 and 13 μm for the diameters of the micro-fibers provided sufficiently separated spectral components avoiding crosstalk during the peak drift in the immersion. We placed the sensors in series and connected to the same input and output interrogator channels previously used in the characterization of single sensors. Fig. 9a) shows the optical spectrum response of the set of sensors distributed in series, and Fig. 9b) shows its FFT magnitude calculation result. The main peak for each sensor in the FFT spectrum were located at 0.14, 0.20 and 0.24 nm⁻¹.

The validation of the multiplexing system was fulfilled by exciting one of the sensors with a progressive immersion keeping the rest unexcited out of the liquid recipient. Fig. 10 shows the tracked SF and phase of the three sensors in the immersion test of S3. Results evidence a good performance of the multiplexing scheme with a maximum crosstalk of 0.2 rad/mm between sensors. Sensors showed phase sensitivities of 1.2, 1.7 and 3 rad/mm, and SF sensitivities of 0.25, 0.5 and 1.25 pm⁻¹/mm.

6. Conclusion

The multiplexing of several liquid level optical sensors is proposed and experimentally demonstrated. Transducers are based on the bimodal interference of the main cylindrical guided modes in optical micro-fibers obtained by the biconical tapering of standard SMF. The shape and length of the tapering is designed in order to provide an effective and efficient power transfer between the guided core mode
of the SMF and the cylindrical second order mode in both tapered fibers. The measurement of the immersed tapered fiber is realized by first interrogating the sensor to obtain the optical spectrum of the bi-modal interferences, then calculating its FFT in real time and finally tracking the SF and phase of the main peaks. Simulations have been performed to fully characterize the sensors sensitivity to the spatial frequency and phase as a function of the width of the micro-fiber, the most sensitive parameter in the system. Micro-fibers with the lowest diameters present phase sensitivities as high as 11.4 rad/mm. The SF domain is finally used to multiplex three sensors with different waist diameters in the same channel of the interrogator. Low crosstalk and the predicted sensitivities are obtained for each sensor. The proposed system disposes additional channels in the interrogator that could be used for the compensation of the effect of temperature if needed.

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CRediT authorship contribution statement

Marko Galarza: Conceptualization, Methodology, Validation, Formal analysis, Investigation, Data Curation, Writing - original draft, Writing - review & editing, Visualization. Rosa Ana Perez-Herrera: Methodology, Validation, Formal analysis, Investigation, Writing - review & editing, Visualization. Aitor Judez: Validation, Formal analysis, Investigation. Manuel López-Amo: Conceptualization, Methodology, Validation, Formal analysis, Resources, Writing - review & editing, Visualization, Supervision, Project administration, Funding acquisition.

Declaration of Competing Interest

None.

References


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