



Article

# Modeling of Surface Roughness in Honing Processes by Using Fuzzy Artificial Neural Networks

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**Abstract:** Honing processes are abrasive machining processes which are commonly employed to improve the surface of manufactured parts such as hydraulic or combustion engine cylinders. These processes can be employed to obtain a cross-hatched pattern on the internal surfaces of cylinders. In this present study, fuzzy artificial neural networks are employed for modeling surface roughness parameters obtained in finishing honing operations. As a general trend, main factors influencing roughness parameters are grain size and pressure. Mean spacing between profile peaks at the mean line parameter, on the contrary, depends mainly on tangential and linear velocity. Grain Size of 30 and pressure of 600 N/cm<sup>2</sup> lead to the highest values of core roughness (R<sub>k</sub>) and reduced valley depth (R<sub>vk</sub>), which were 1.741 μm and 0.884 μm, respectively. On the other hand, the maximum peak-to-valley roughness parameter (R<sub>z</sub>) so obtained was 4.44 μm, which is close to the maximum value of 4.47 μm. On the other hand, values of the grain size equal to 14 and density equal to 20, along with pressure 600 N/cm<sup>2</sup> and both tangential and linear speed of 20 m/min and 40 m/min, respectively, lead to the minimum values of core roughness, reduced peak height (R<sub>pk</sub>), reduced valley depth and maximum peak-to-valley height of the profile within a sampling length, which were, respectively, 0.141 μm, 0.065 μm, 0.142 μm, and 0.584 μm.

**Keywords:** roughness; honing; ANFIS; modeling; kurtosis; skewness



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## 1. Introduction

The surface texture of the cylinder liners influences greatly the performance of combustion engines, especially regarding friction, oil consumption, emissions, wear, etc. [1]. It also affects the ring-pack performance [2]. Specifically, the honing angle has a great impact on the friction coefficient in the liner-ring pair. In general, low coefficient of friction is obtained when a low honing angle is employed, for example 40° [3].

In order to analyze and compare different surface topographies, several roughness parameters have previously been used in honing processes. In [4], Buj et al. employed regression models to predict roughness, material removal rate and tool wear in the rough, semi-finish and finish operations. They found that roughness is mainly influenced by grain size and density of abrasive. A sensitivity analysis was presented in their study for a multi-objective optimization process. In Kanthababu et al. [5] the surface topography was characterized by average roughness (R<sub>a</sub>) and all five bearing area parameters ((R<sub>pk</sub>), (R<sub>k</sub>), (R<sub>vk</sub>), (Mr<sub>1</sub>) and (Mr<sub>2</sub>)). These authors found that R<sub>a</sub> can be replaced effectively by R<sub>k</sub> in finishing honing operations to control the final surface topography. Barros et al. [6] studied the influence of grain size and of the number of strokes on the bearing area parameters in flexible honing. They observed that grain size influenced mainly parameters (R<sub>k</sub>), (R<sub>pk</sub>), (Mr<sub>2</sub>), and (R<sub>p</sub>/R<sub>t</sub>), while the number of strokes influenced (R<sub>pk</sub>). Sadizade et al. [7]

studied the (Rk) family parameters in plateau honing operations of Diesel engines. They define a two-stage process (instead of the usual three-stage process) containing rough honing (with the consecutive application of high and low pressure) and plateau honing, in which total honing time is thus reduced. (Rpk) parameter depends mainly on low pressure, low time and plateau pressure. (Rk) depends on low pressure, plateau pressure and the plateau stroke number. (Rvk) depends on low pressure and low time. Thus, low pressure is an important variable affecting the three a.m. parameters. Ma et al. [8] studied the plateau honing operation of CuNiCr iron liners [8] and observed that a honing angle of  $58^\circ$  implies better tribological properties for the liners. In addition, they observed that the tribological properties are more related to parameters Rk and Rpk than to parameter Ra.

High correlations between roughness parameters are found in honing processes. Deepak Lawrence et al. [9] predicted the bearing area parameters from images of the honed surfaces. They found high correlation between the Rk family parameters determined with an image instrument and the same parameters measured with a stylus instrument. Highest correlation values of 0.81 and 0.82 were reported for Rpk and Spk parameters, respectively, which are related to the profile peaks. Pawlus et al. [10] studied the plateau-honing process and found correlations between the (Rk) family parameters and the (Rq) family parameters. They found that (Rmr1) and (Rmr2) are strongly correlated with (Rmq), and that the peak parameters (and the valley parameters) of the two families are also correlated.

Other roughness parameters that are related to the shape of the profile, such as kurtosis (Rku) or skewness (Rsk) are useful in one-stage processes such as honing [11]. For example, they allow monitoring wear of the cylinder surface [12]. Both parameters are known to be correlated and, for this reason, they are not recommended in two-stage processes like plateau-honing [13]. In Gaussian ordinate distributions, (Rsk) is usually close to 0, while (Rku) is similar to 3 [13]. Areal (Sku) and (Ssk) parameters were determined in semi-finishing honing processes by Buj-Corral et al. [14]. They found (Ssk) values similar to 0 and (Sku) values above 3 in all cases.

Spacing roughness parameters such as the mean width of roughness profile (RSm) have been reported to decrease in superfinishing operations [15]. In general, parameter (RSm) depends on the size of the scratches produced by the grains in abrasive machining processes, for example in belt finishing [16]. In plateau honing processes, Pawlus et al. [17] observed that, after applying a Gaussian filter to the roughness signal, the (RSm) parameter decreased.

Design of experiments (DOE) combined with artificial neural networks (ANN) have been widely used over the last few years to analyze the behavior of different output variables. In the literature, several studies can be found that deal with the application of soft computing for the modelling of different manufacturing processes. For example, the research study by Lalwani et al. [18] compared response surface methodology (RSM) and ANN for modeling the wire electrical discharge machining (WEDM) process. Among their results, these authors found that ANN had higher accuracy than RSM. Likewise, in Mirifar et al. [19] a feedforward neural network and Bayesian backpropagation algorithm were used to predict forces and roughness in grinding processes by using an acoustic emission sensor. These authors found, among their results, that ANNs were able to model obtained roughness with high precision. As for honing processes, Buj et al. [20] obtained an adaptive indirect ANN model in which the values of the process parameters are predicted from the measured Rk, Rpk and Rvk values.

On the other hand, fuzzy artificial neural networks (ANFIS) have also been employed to model machining processes. In a study from Aamir et al. [21] Taguchi design of experiments and fuzzy logic were employed to predict surface roughness and hole size in multi-hole drilling. Furthermore, in the work by Alajmi et al. [22], surface roughness obtained in dry and cryogenic turning of AISI 304 stainless steel was modeled using ANFIS-QPSO (fuzzy artificial neural networks with quantum particle swarm optimization). These authors found that ANFIS-QPSO was an effective and highly accurate method. Shivakoti et al. [23] analyzed the influence of feed, speed, and depth of cut on material removal rate,

surface roughness and cutting force, in turning EN31 alloy steel by using ANFIS models. These authors found that ANFIS had high accuracy in predicting the output variables analyzed in their study. Regarding abrasive machining processes, Nguyen et al. [24] used the ANFIS-GPR (fuzzy artificial neural networks with gaussian process regression) hybrid algorithm with Taguchi analysis to model surface roughness in grinding operations. The ANFIS-GPR algorithm provided better predictability than ANFIS and Taguchi.

In this work, ANFIS models are applied to roughness parameters in finishing honing processes. It will help to select appropriate process parameters to improve obtained roughness within the current range of variation and parameters considered. Different roughness parameters are considered, including the (Rk) family parameters, kurtosis (Rku), skewness (Rsk) and the mean width of the roughness profile (RSm), which has been scarcely studied in the literature about honing processes. In addition, the application of ANFIS models to honing processes allows obtaining models with high fit values for the different roughness parameters.

The remaining sections of this present study are structured as follows: Section 2 corresponds to materials and methods; Section 3 contains the results and discussion; and in Section 4 the main conclusions of the work are presented.

## 2. Materials and Methods

In this section the methodology and the experiments carried out for modeling the honing process are outlined.

### 2.1. Research Methodology

To obtain the relationship between the response variables and the input variables, a set of experiments was carried out. These experiments were defined according to a two-level fractional factorial design  $2^{5-1}$  with three center points, as shown in Table 1. The levels of variation in the input variables were selected considering the experience of the authors in similar processes. The input variables considered in this study were particle size, density, pressure, and both tangential and linear velocity, since these are the parameters that most influence the response variables to be analyzed.

**Table 1.** Levels of the input variables.

	Input Variables		Low	Center	High
GS:	Grain Size	(ISO 6106 [25])	15	20	30
DE:	Density	(ISO 6104 [26])	10	15	20
PR:	Pressure	(N/cm <sup>2</sup> )	400	500	600
TV:	Tangential Speed	(m/min)	20	30	40
LV:	Linear Speed	(m/min)	20	30	40

The output variables (response variables) analyzed in this study were: Core Roughness (Rk (μm)), Reduced peak height (Rpk (μm)), Reduced valley depth (Rvk (μm)), Material ratio (Mr1 (%) and Mr2 (%)), Maximum peak-to-valley height of the profile within a sampling length (Rz (μm)), Skewness (Rsk), Kurtosis (Rku) and Mean spacing between profile peaks at the mean line (RSm (μm)). That is, all five bearing area parameters (Rpk, Rk, Rvk, Mr1 and Mr2) were considered and, additionally, Rz, Rsk, Rku and RSm were analyzed in this present study as output variables.

As mentioned in the Section 1, in Kanthababu et al. [5] it was found that Ra can effectively be replaced by (Rk) in finishing honing operations to control the final surface topography. All bearing parameters, and (Rsk), (Rku) and (RSm) were also considered because these are the most useful parameters to analyze the honed parts. Therefore, these are the parameters whose influence is to be analyzed in this study.

As mentioned in the Section 1, it was found in M. Kanthababu et al. [5] that Ra can be effectively replaced by (Rk) in finish honing operations to control the final surface topography, and all bearing parameters and (Rsk), (Rku) and (RSm) were also taken into account because these are the most useful parameters to analyze honed parts. Therefore, these are the parameters whose influence will be analyzed in this study

Regarding the set-up of the experiments required to carry out the honing process, a horizontal test honing machine was employed from Honingtec S.A. Steel St-52 cylinders of internal diameter 50 mm and length 150 mm were employed, as Figure 1 shows.



**Figure 1.** Steel St-52 cylinders.

In this present study cBN honing stones with metallic bond were used, as can be observed in Figure 2.



**Figure 2.** cBN honing stones.

Once the experiments were planned, the different honed conditions were employed to different cylinders, and then the surface roughness were measured on the manufactured parts, as explained in Section 2.2. From these results, a FIS was developed and then the parameters of the FIS's membership functions were tuned by using an ANFIS. Then the obtained results were discussed and compared with those reported by other researchers found in the specialized bibliography dealing with honing.

## 2.2. Surface Roughness Measurements

Roughness was measured with a Taylor Hobson Talysurf 2 contact roughness meter, as shown in Figure 3, with a Gaussian filter with cut-off value of 0.8 mm. Evaluation length was 4 mm. A diamond tip was used with tip radius of 2  $\mu\text{m}$  and tip angle of 90°. Resolution of the inductive sensor was 18 nm and the measuring force was 1 mN.





Figure 3. Taylor Hobson Talysurf 2 contact roughness meter.

Measurement results obtained in the honing test are presented in Table 2. The results for average roughness (Ra) are not included in this study and will be presented elsewhere.

Table 2. Results of the honing tests.

#	GS	DE	PR	TV	LV	Rk	Rpk	Rvk	Mr1	Mr2	Rz	Rsk	Rku	RSm
1	15	20	400	20	20	0.175	0.077	0.175	8.380	83.168	0.768	−1.280	7.417	35.558
2	15	20	600	40	20	0.294	0.100	0.191	8.120	87.120	0.976	−0.817	6.688	31.468
3	15	20	600	20	40	0.141	0.065	0.142	8.168	84.508	0.584	−2.061	18.145	59.563
4	15	20	400	40	40	0.323	0.143	0.219	9.050	87.355	1.234	−0.634	8.479	39.895
5	15	10	600	20	20	0.231	0.112	0.322	8.193	84.485	1.222	−2.217	14.766	52.478
6	15	10	400	40	20	0.191	0.080	0.183	8.025	84.343	0.876	−1.333	9.008	36.233
7	15	10	400	20	40	0.232	0.142	0.264	8.613	83.725	0.923	−1.140	9.526	56.975
8	15	10	600	40	40	0.225	0.131	0.223	8.490	84.218	0.954	−0.752	8.253	40.108
9	30	20	600	20	20	1.552	0.781	0.674	10.778	88.875	3.803	0.237	3.599	47.790
10	30	20	400	40	20	0.588	0.275	0.400	9.880	88.205	2.211	−0.525	6.241	44.748
11	30	20	400	20	40	1.090	0.493	0.488	9.885	89.493	2.660	0.023	4.216	69.445
12	30	20	600	40	40	1.741	0.750	0.884	10.260	88.998	4.439	−0.025	3.837	48.318
13	30	10	400	20	20	0.737	0.460	0.466	9.948	87.605	2.504	−0.085	6.157	55.480
14	30	10	600	40	20	1.682	0.807	0.752	10.808	89.420	4.470	0.129	3.651	39.013
15	30	10	600	20	40	1.629	0.719	0.756	11.060	89.405	3.794	−0.079	4.018	75.640
16	30	10	400	40	40	0.757	0.370	0.385	8.188	88.000	2.127	−0.136	4.546	47.088
17	20	15	500	30	30	0.518	0.280	0.306	9.150	87.493	1.639	−0.193	4.794	37.233
18	20	15	500	30	30	0.715	0.323	0.411	9.925	86.613	2.104	−0.170	4.282	50.043
19	20	15	500	30	30	0.729	0.353	0.425	9.233	87.635	2.355	−0.147	4.780	51.618

The results shown in Table 2 were employed to develop the FIS and then optimized by an ANFIS as shown in the next section.

### 2.3. FIS Modeling

Figure 4 shows the membership functions for fuzzification of the five different inputs, which are based on a Gaussian function as Equation (1) shows:

$$\mu = e^{-\frac{(x-c)^2}{2\sigma^2}} \tag{1}$$

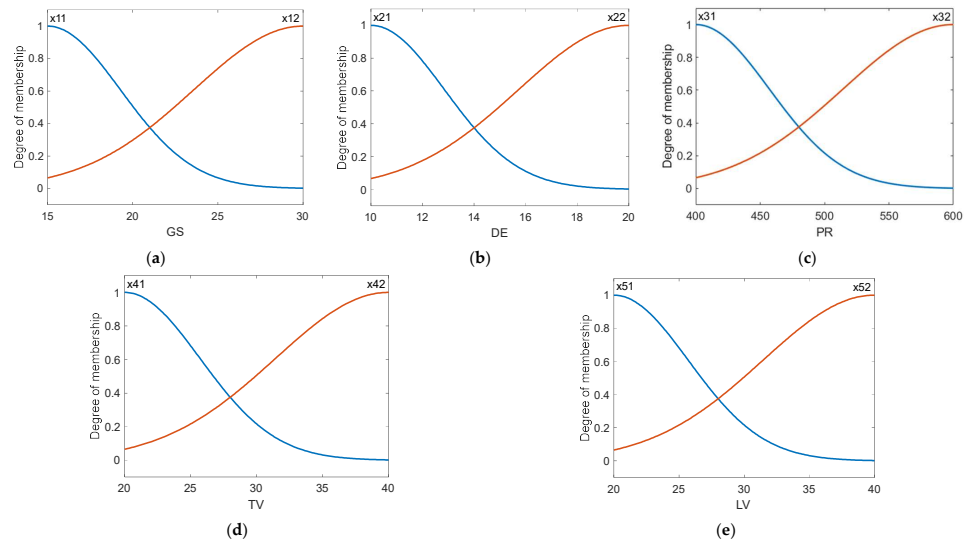


Figure 4. Membership functions for fuzzification of the inputs for: (a) GS; (b) DE; (c) PR; (d) TV; (e) LV.

To develop the FIS, the first sixteen results of the honing experiments shown in Table 2 were used. Figure 4 shows the membership functions for fuzzification of the inputs. These functions can be obtained after substituting the values shown in Table 3, in Equation (1), for each of the input variables considered in the present study, respectively. The membership functions' values are show in Table 3. These values were selected from the procedure explained in [27]. In this study the Gaussian membership functions were implemented by using the Fuzzy Logic Toolbox™ of Matlab™2020a [24].

Table 3. Values of the membership functions employed to develop the FISs.

[Input1]	[Input2]	[Input3]
Name = 'GS' Range = [15 30] MF1 = 'x1':'gaussmf', [4.2857 15] MF2 = 'x12':'gaussmf', [6.4286 30]	Name = 'DE' Range = [10 20] MF1 = 'x21':'gaussmf', [2.8571 10] MF2 = 'x22':'gaussmf', [4.2857 20]	Name = 'PR' Range = [400 600] MF1 = 'x31':'gaussmf', [57.1429 400] MF2 = 'x32':'gaussmf', [85.7143 600]
[Input4]	[Input5]	
Name = 'TV' Range = [20 40] MF1 = 'x41':'gaussmf', [5.7143 20] MF2 = 'x42':'gaussmf', [8.5714 40]	Name = 'LV' Range = [20 40] MF1 = 'x51':'gaussmf', [5.7143 20] MF2 = 'x52':'gaussmf', [8.5714 40]	

The aggregation method employed is the sum of fuzzy sets. In this present case, the aggregated output is obtained from the weighted average of all output rules. Both the implication method and the output of the Sugeno FIS are shown in Equations (2) and (3) [27–29]:

$$w_j(x) = \text{AndMethod}\{\mu_1(x_1), \dots, \mu_n(x_n)\} \tag{2}$$

$$\text{output}_j = \frac{\sum_{j=1}^{\text{Number of rules}} w_j * z_j}{\sum_{j=1}^{\text{Number of rules}} w_j} \tag{3}$$

As previously mentioned, zero-order Sugeno FISs were developed for each of the output variables, where output corresponds to Rk, Rpk, Rvk, Mr1, Mr2, Rz, Rsk, Rku and RSm. Each of the FISs have a set of n rules of the form shown by Equation (4), where x<sub>i</sub> (i = 1,2,...5) corresponds to the independent variable, and z<sub>j</sub> corresponds to the output

obtained in each experiment and two membership functions are selected for each of the independent variables ( $k = 1, 2$ ), as previously mentioned.

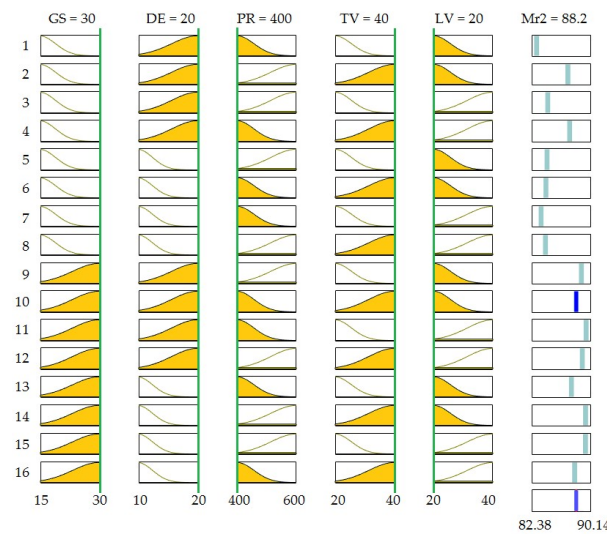
$$\text{if } ((x_1 \text{ is } x_{1k}) \text{ and } (x_2 \text{ is } x_{2k}) \text{ and } \dots \text{ and } (x_5 \text{ is } x_{5k})) \text{ then output}_j \text{ is } z_j \quad (4)$$

Table 4 shows the rules that have been employed in this present study which have been developed from Equation (3) and from the experimental data shown in Table 3.

**Table 4.** Rules of the FIS.

#	Rule
1	$(x_1 = x_{11}) \& (x_2 = x_{22}) \& (x_3 = x_{31}) \& (x_4 = x_{41}) \& (x_5 = x_{51}) \Rightarrow z_1$
2	$(x_1 = x_{11}) \& (x_2 = x_{22}) \& (x_3 = x_{32}) \& (x_4 = x_{42}) \& (x_5 = x_{51}) \Rightarrow z_2$
3	$(x_1 = x_{11}) \& (x_2 = x_{22}) \& (x_3 = x_{32}) \& (x_4 = x_{41}) \& (x_5 = x_{52}) \Rightarrow z_3$
4	$(x_1 = x_{11}) \& (x_2 = x_{22}) \& (x_3 = x_{31}) \& (x_4 = x_{42}) \& (x_5 = x_{52}) \Rightarrow z_4$
5	$(x_1 = x_{11}) \& (x_2 = x_{21}) \& (x_3 = x_{32}) \& (x_4 = x_{41}) \& (x_5 = x_{51}) \Rightarrow z_5$
6	$(x_1 = x_{11}) \& (x_2 = x_{21}) \& (x_3 = x_{31}) \& (x_4 = x_{42}) \& (x_5 = x_{51}) \Rightarrow z_6$
7	$(x_1 = x_{11}) \& (x_2 = x_{21}) \& (x_3 = x_{31}) \& (x_4 = x_{41}) \& (x_5 = x_{52}) \Rightarrow z_7$
8	$(x_1 = x_{11}) \& (x_2 = x_{21}) \& (x_3 = x_{32}) \& (x_4 = x_{42}) \& (x_5 = x_{52}) \Rightarrow z_8$
9	$(x_1 = x_{12}) \& (x_2 = x_{22}) \& (x_3 = x_{32}) \& (x_4 = x_{41}) \& (x_5 = x_{51}) \Rightarrow z_9$
10	$(x_1 = x_{12}) \& (x_2 = x_{22}) \& (x_3 = x_{31}) \& (x_4 = x_{42}) \& (x_5 = x_{51}) \Rightarrow z_{10}$
11	$(x_1 = x_{12}) \& (x_2 = x_{22}) \& (x_3 = x_{31}) \& (x_4 = x_{41}) \& (x_5 = x_{52}) \Rightarrow z_{11}$
12	$(x_1 = x_{12}) \& (x_2 = x_{22}) \& (x_3 = x_{32}) \& (x_4 = x_{42}) \& (x_5 = x_{52}) \Rightarrow z_{12}$
13	$(x_1 = x_{12}) \& (x_2 = x_{21}) \& (x_3 = x_{31}) \& (x_4 = x_{41}) \& (x_5 = x_{51}) \Rightarrow z_{13}$
14	$(x_1 = x_{12}) \& (x_2 = x_{21}) \& (x_3 = x_{32}) \& (x_4 = x_{42}) \& (x_5 = x_{51}) \Rightarrow z_{14}$
15	$(x_1 = x_{12}) \& (x_2 = x_{21}) \& (x_3 = x_{32}) \& (x_4 = x_{41}) \& (x_5 = x_{52}) \Rightarrow z_{15}$
16	$(x_1 = x_{12}) \& (x_2 = x_{21}) \& (x_3 = x_{31}) \& (x_4 = x_{42}) \& (x_5 = x_{52}) \Rightarrow z_{16}$

As previously mentioned, once the Sugeno FIS were developed an ANFIS was used to adjust the membership functions' parameters by using the Fuzzy Logic Toolbox™ of Matlab™2020a [28]. As an example, Figure 5 shows the output of the ANFIS for experiment number 10 in the case of Mr2. In order to optimize the values of the membership functions, the optimization type was "tuning" and the method "anfis". To obtain these tuned FIS, all the experimental data were employed. Detailed information about the algorithm employed by the ANFIS can be found in the research study of Jang [30].



**Figure 5.** Output of the ANFIS model for experiment #10, in the case of Mr2.

### 3. Discussion and Results

As can be seen in Table 2, as a general trend, lower (Rk), (Rpk), (Rvk) and (Rz) values were obtained in the first 8 experiments, corresponding to low grain size, than in

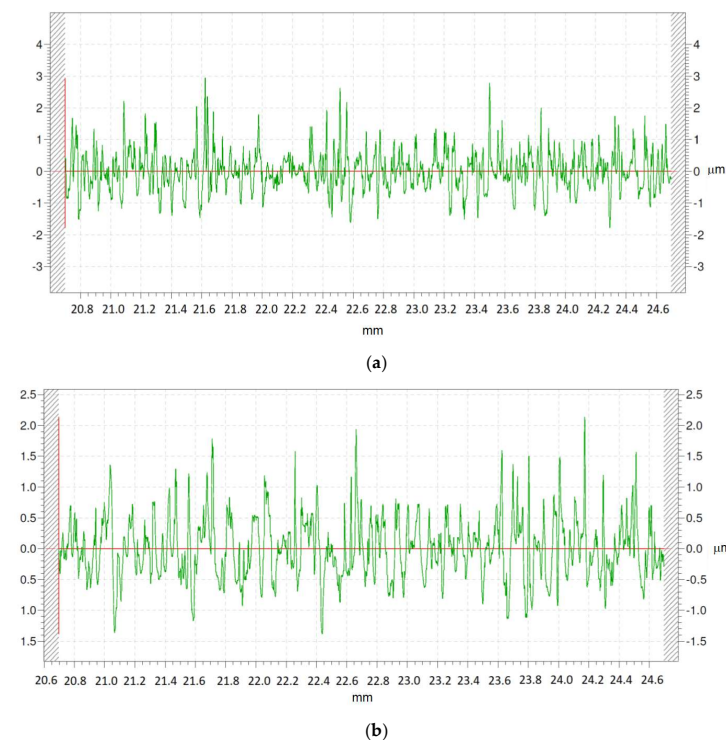
experiments 9 to 16, corresponding to high grain size. In plateau-honing experiments with diamond stones, Lawrence et al. [9] reported higher ( $R_k$ ) values up to  $2.25\ \mu\text{m}$  and higher ( $R_{vk}$ ) values up to  $2.06\ \mu\text{m}$ . They also obtained lower ( $R_{pk}$ ) values up to  $0.55\ \mu\text{m}$ , probably because the plateau operation smoothed the previous peaks.

As for skewness ( $R_{sk}$ ), which measures the symmetry of the profile, mainly negative values were obtained, corresponding to profiles with higher valley depths than peak heights. Experiments 9 to 16, obtained with high grain size of 30, provided ( $R_{sk}$ ) values that are closer to zero and, in some cases, slightly positive up to 0.237 for experiment 9. All the experiments carried out with low grain size of 15 (experiments 1 to 8) showed negative ( $R_{sk}$ ) values, with a low value of  $-2.217$  for experiment 5. As a general trend, a honed surface will show ( $R_{sk}$ ) values that are negative or slightly positive (between  $-1.5$  and  $0.5$  approx.) [31], while a plateau-honed surface will have negative skewness [31,32]. A negative ( $R_{sk}$ ) value favors the retention of fluids by a certain surface [33].

Regarding kurtosis ( $R_{ku}$ ), which evaluates the peakedness of the roughness profile, higher values were obtained for the experiments with grain size 15 (up to more than 18 for experiment 3) than for grain size 30 (below 7 in all cases). High kurtosis is related to sharp peaks. For instance, in honing processes, Kang et al. [12] reported ( $S_{ku}$ ) values of around 3.2 for an unworn surface, which increased with the running-in operation up to more than 10. As a general trend, honing processes provide ( $R_{ku}$ ) ranging from approx. 3 to more than 10 [31], while in plateau-honing ( $R_{ku}$ ) will be higher than 3 [31,32].

As for ( $R_{sm}$ ), as a general trend higher values were reported in this work for grain size 30 (up to  $75\ \mu\text{m}$ ) than for grain size 15 (up to  $59\ \mu\text{m}$ ). The ( $R_{sm}$ ) values obtained are similar to those of  $62.3\ \mu\text{m}$  reported by Grzesik et al. in turning + superfinishing operations [15]. In periodic roughness profiles, for example those obtained in turning and milling operations, ( $R_{sm}$ ) is related to feed [34]. However, in more irregular profiles such as those obtained in abrasive machining processes, ( $R_{sm}$ ) is related to grain size and depth of the grain [35].

Figure 6 provides two different roughness profiles corresponding to experiments 9 and 11. They were both obtained with high grain size of 30 and high density of 20. However, experiment 9 was conducted at high pressure of  $600\ \text{N}/\text{mm}^2$ , while experiment 11 was conducted at low pressure of  $400\ \text{N}/\text{mm}^2$ .

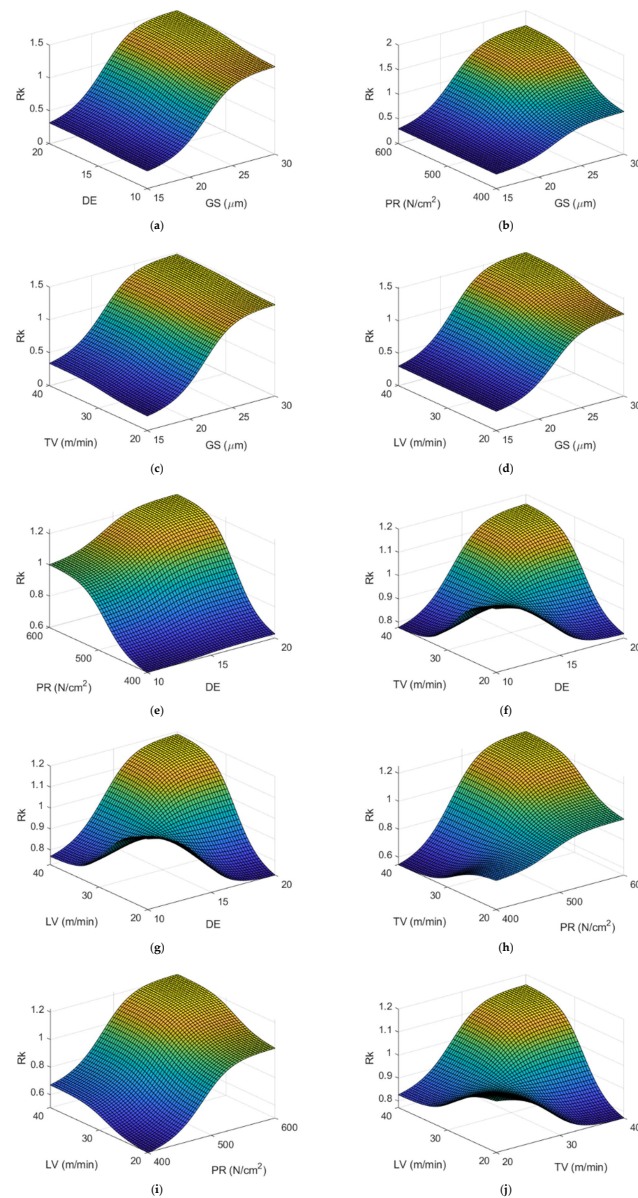


**Figure 6.** Roughness profiles of: (a) Experiment 9, obtained with high pressure of  $600\ \text{N}/\text{cm}^2$ ; (b) Experiment 11, obtained with low pressure of  $400\ \text{N}/\text{cm}^2$ .



Higher peaks (up to 3  $\mu\text{m}$  high) and lower valleys (up to 1.8  $\mu\text{m}$  deep) are obtained with high pressure (Figure 6a) than with low pressure (Figure 6b). This suggests that higher pressure leads to deeper scratch marks on the workpiece's surface [36]. On the other hand, in rough honing processes pressure is known to affect not only roughness but also the cylindricity error of the parts [37].

From the experimental values obtained after the design of experiments deployed in Table 2, a fuzzy inference system was developed for each of the response variables. Once these FISs were obtained, ANFISs were employed to adjust the values of the membership functions in order to obtain greater precision in the models thus obtained. The results obtained are shown below. As can be observed, Figure 7 shows the response surface plots for (Rk), for different pairs of variables, which have been obtained by using the ANFIS, where two independent variables are varied within their variation levels while the rest are kept at their central values.



**Figure 7.** Response surface for (Rk ( $\mu\text{m}$ )) versus each pair of input variables while the rest are kept at their central values, using the ANFIS developed for (Rk): (a) GS and DE; (b) GS and PR; (c) GS and TV; (d) GS and LV; (e) DE and PR; (f) DE and TV; (g) DE and LV; (h) PR and TV; (i) PR and LV; (j) TV and LV.

Similarly, Figure 8 depicts the main effects plot and the interaction plots for (Rk). The main effects plot is obtained from the variation in a variable between its lower and upper limits, while the remaining ones are kept at their central values and the interaction effects plot is obtained for each pair of variables, while the others are kept at their central values. This procedure is followed for all roughness parameters considered in the present study.

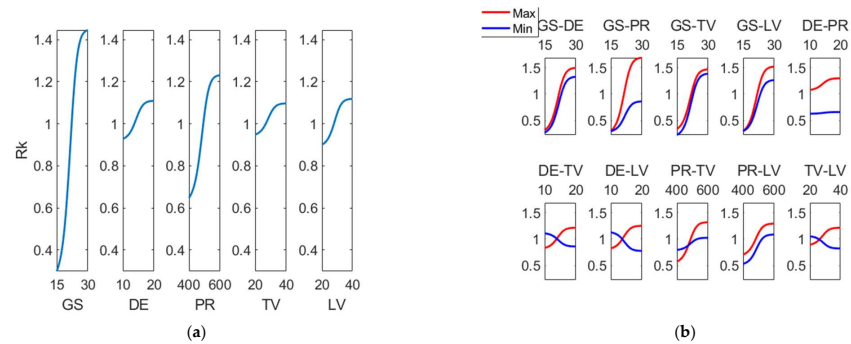


Figure 8. (a) Main effects plot and (b) interaction effects plot for ( $R_k$  ( $\mu\text{m}$ )).

In Figure 8 it can be observed that the main factor influencing ( $R_k$ ) parameter is grain size (GS), followed by pressure (PR). As for the interactions, most significant ones are related to parameter GS, for example, GS-DE, GS-PR, GS-TV and GS-LV. Caetano Barros et al. observed that ( $R_k$ ) in honing processes is greatly dependent on grain size [6]. They used mesh sizes of 400 and 800, respectively. For example, mesh size of 400 in the Norton scale corresponds to particle size of around  $46 \mu\text{m}$  (semifinishing honing).

Likewise, Figure 9 contains the main effects plot as well as the interaction effects plot for reduced peak height ( $R_{pk}$ ). As can be observed, the main factors affecting roughness are grain size (GS) and pressure (PR), while main interactions are GS-DE, GS-PR, GS-TV and GS-LV. This behavior is similar to that of the ( $R_k$ ) parameter. These results are in accordance with those of Caetano Barros et al. [6], who found a great influence of grain size on ( $R_{pk}$ ) parameter. On the other hand, Figure 10 depicts the main effects plot and the interaction effects plot for ( $R_{vk}$ ). Main effects for reduced peak height ( $R_{vk}$ ) are grain size and pressure, and the most significant interactions are GS-DE, GS-PR, GS-TV and GS-LV. On the contrary, Caetano Barros et al. reported that ( $R_v$ ) parameter remained almost unchanged when grain size was varied [6].

Figure 11 corresponds to the surface response plots for ( $Mr_1$ ) and Figure 12 depicts both the main effect plot and the interaction effects plot for ( $Mr_1$ ). It can be observed that the main effect for ( $Mr_1$ ) is grain size (GS), followed by pressure (PR). Most significant interactions correspond to GS with all the other variables, as well as DE-PR.

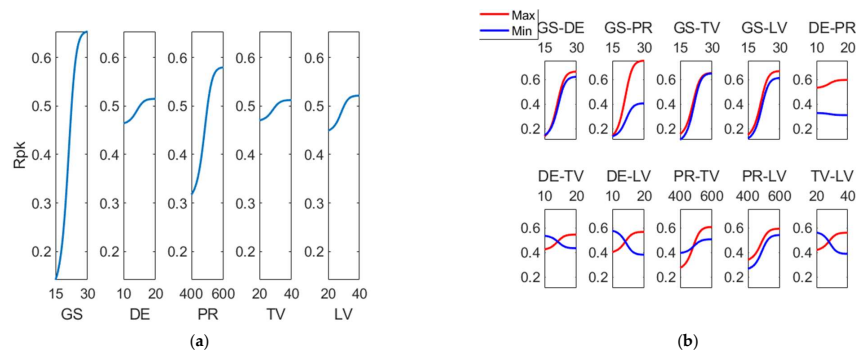


Figure 9. (a) Main effects plot and (b) interaction effects plot for ( $R_{pk}$  ( $\mu\text{m}$ )).

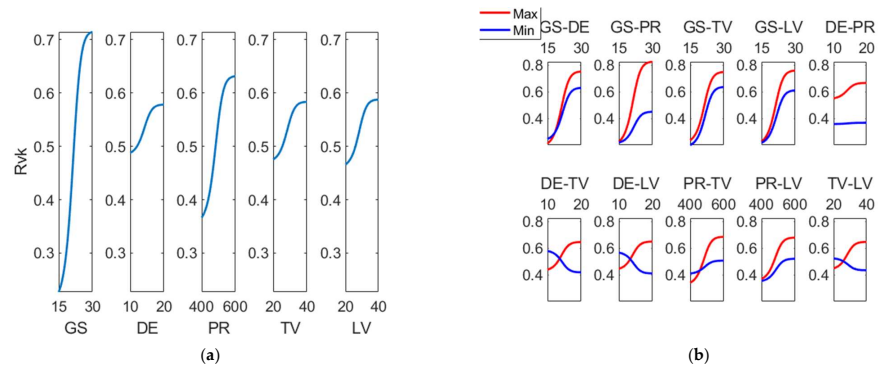


Figure 10. (a) Main effects plot and (b) interaction effects plot for (Rvk (μm)).

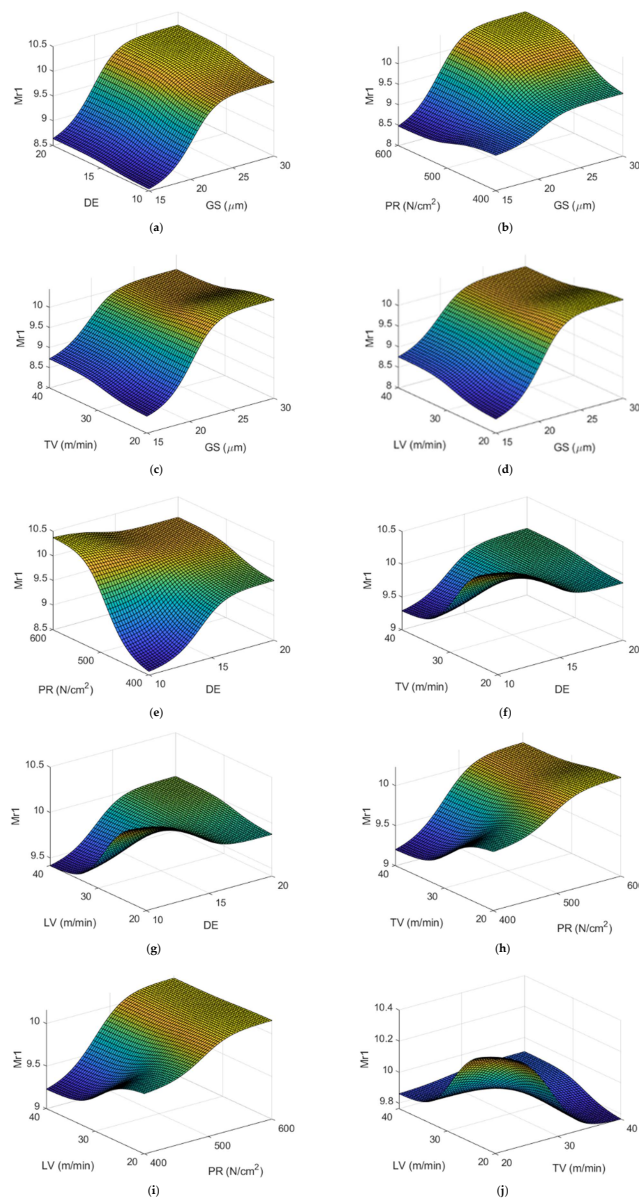


Figure 11. Response surface for (Mr1 (%)) versus each pair of input variables while the rest are kept at their central values, using the ANFIS developed for (Mr1): (a) GS and DE; (b) GS and PR; (c) GS and TV; (d) GS and LV; (e) DE and PR; (f) DE and TV; (g) DE and LV; (h) PR and TV; (i) PR and LV; (j) TV and LV.

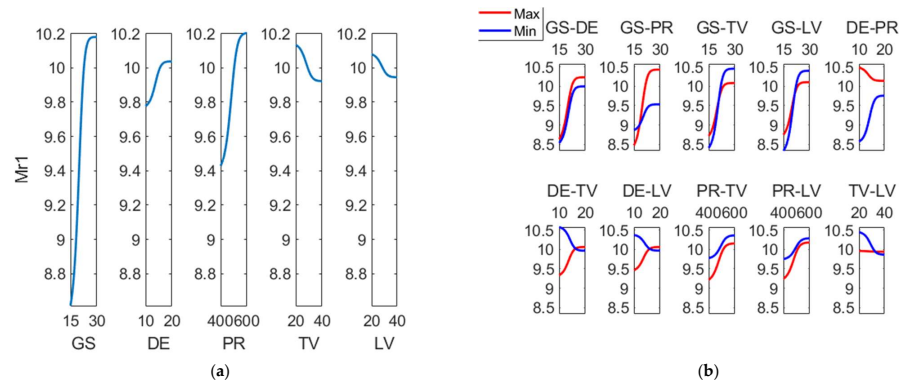


Figure 12. (a) Main effects plot and (b) interaction effects plot for Mr1 (%).

Figure 13 depicts the main effects and the interaction effects plot for (Mr2). As can be observed, the main effect for (Mr2) is grain size. On the other hand, most significant interactions correspond to GS-DE, GS-PR, GS-TV and GS-LV. Anderberg et al. found a great correlation between (Mr1) and (Mr2) in honing processes [38].

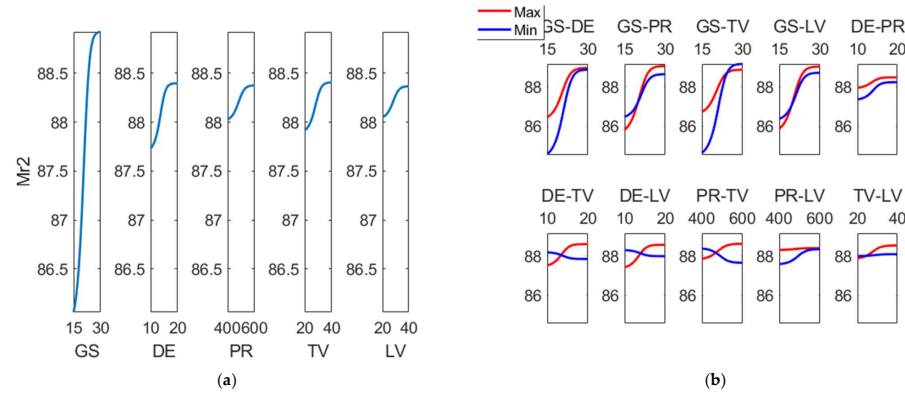


Figure 13. (a) Main effects plot and (b) interaction effects plot for (Mr2 (%)).

Figure 14 corresponds to the main effects plot and the interactions effect plot for (Rz). As with (Rk), the main factors are GS and PR, and the main interactions are those related to GS.

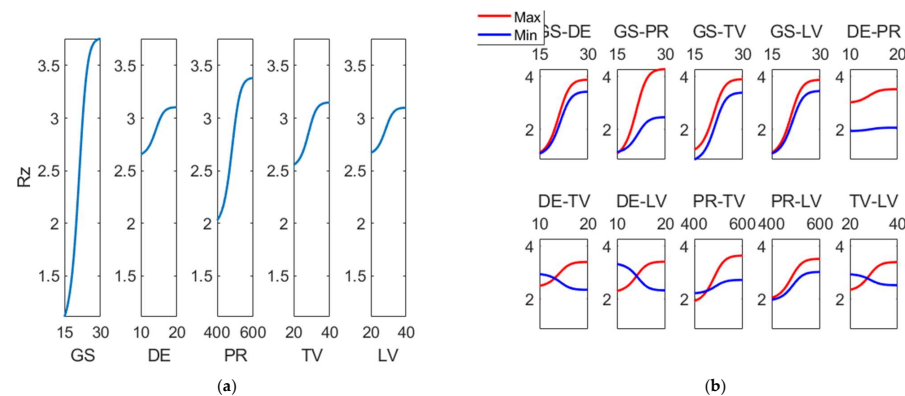


Figure 14. (a) Main effects plot and (b) interaction effects plot for Rz (μm).

Figure 15 corresponds to the main effects plot and the main interactions plot for (Rsk). It can be observed that the main effect for (Rsk) is grain size, followed distantly by pressure. Most significant interactions correspond to those of (GS) with all the other variables. In this work, (Rsk) increases with grain size. Conversely, in the grinding processes of Inconel, (Rsk), a larger grit size results in lower (more negative) (Rsk) values [39]. In polishing operations of copper parts, the corresponding areal skewness parameter (Ssk) decreases slightly with grain size up to a certain grain size value from which it increases [40].



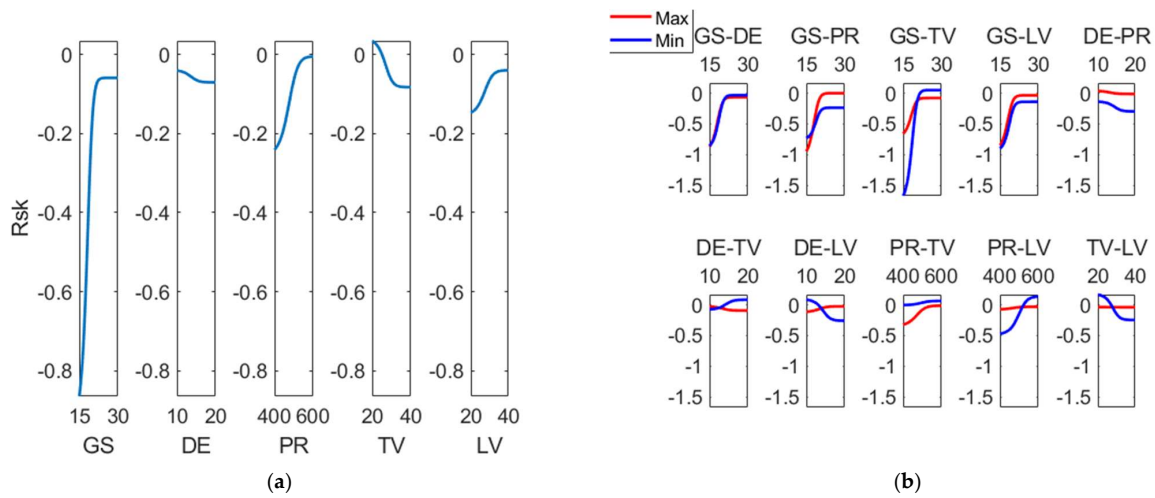


Figure 15. (a) Main effects plot and (b) interaction effects plot for ( $R_{sk}$ ).

Figure 16 shows the main effects plot and the main interactions plot for skewness kurtosis ( $R_{ku}$ ). Main effect for ( $R_{ku}$ ) is grain size, followed by pressure. Most significant interactions correspond to (GS) with all the other variables. As a general trend, in grinding processes kurtosis is more related to grain size than to the cutting conditions [41]. In this work, ( $R_{ku}$ ) decreases with grain size. Conversely, in grinding processes of Inconel, ( $R_{ku}$ ) increases with grain size [39]. In polishing operations of copper parts, the corresponding areal kurtosis parameter ( $S_{ku}$ ) decreases slightly with grain size up to a certain grain size value and then increases [40].

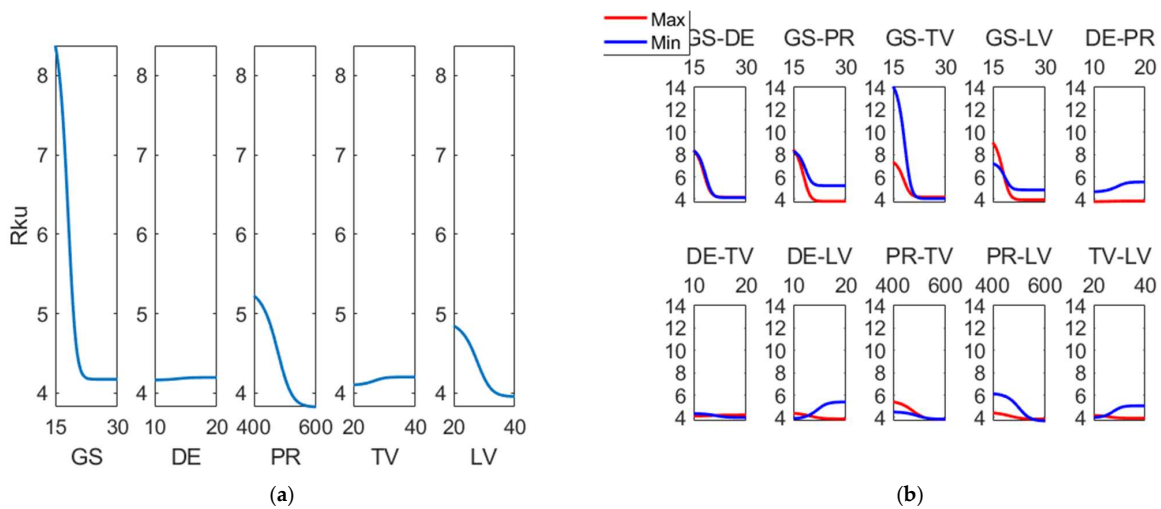


Figure 16. (a) Main effects plot and (b) interaction effects plot for  $R_{ku}$ .

The main effects plot and the main interactions plot for ( $R_{Sm}$ ) can be observed in Figure 17. Contrary to what happens to the rest of the responses, in this case main effect is tangential velocity (TV), followed by linear velocity (LV) and by grain size (GS). Main interaction effects correspond to those related to TV, like GS-TV, DE-TV, PR-TV and TV-LV. Parameter ( $R_{Sm}$ ) was reported to decrease after belt grinding and superfinishing (with honing stones) [15].

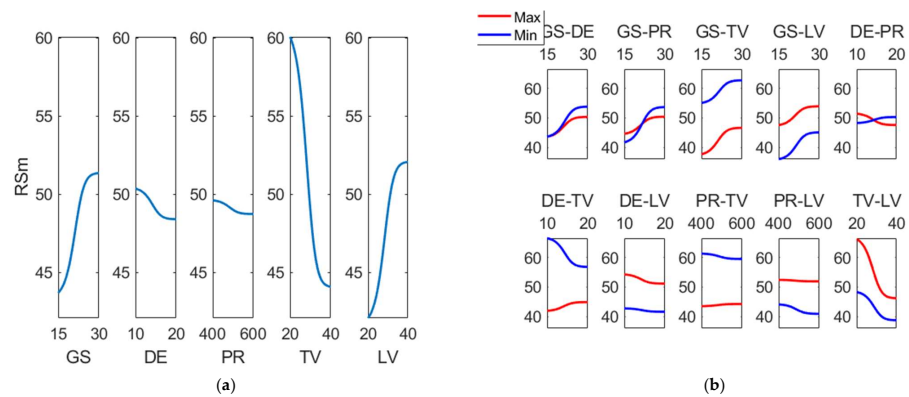


Figure 17. (a) Main effects plot and (b) interaction effects plot for RSm (μm).

#### 4. Conclusions

In this present study an analysis of all five bearing area parameters (Rpk), (Rk), (Rvk), (Mr1) and (Mr2), and additionally (Rz), (Rsk), (Rku) and (RSm) have been analyzed by using fuzzy inference systems and artificial neural fuzzy inference systems, where five design parameters were considered as input variables (GS, DE, PR, TV, LV).

It was found that the models thus obtained allow predicting the behavior of the response variables with a high degree of accuracy within the current range of variation and parameters considered.

On the other hand, it was shown that in all response variables except for (RSm) the main affecting parameter is grain size (GS), which could be related to the fact that the finishing honing operation is the main objective of this study. Grain Size of 30 and pressure of 600 N/cm<sup>2</sup> lead to the highest values of core roughness (Rk) and reduced valley depth (Rvk), which were 1.741 μm and 0.884 μm, respectively. On the other hand, the maximum peak-to-valley height of the profile parameter (Rz) so obtained was 4.44 μm, which is close to the maximum value of 4.47 μm.

On the other hand, values of the grain size equal to 15 and density equal to 20, along with pressure 600 N/cm<sup>2</sup> and both tangential and linear speed of 20 m/min and 40 m/min, respectively, lead to the minimum values of core roughness, reduce peak height, reduced valley depth and maximum peak-to-valley height of the profile within a sampling length; these were, respectively, 0.141 μm, 0.065 μm, 0.142 μm, and 0.584 μm.

In general, it has been observed that the main parameter affecting the results in this study, except for (RSm), is grain size (GS), followed by pressure (PR). As for the interactions, the most significant ones are related to the (GS) parameter, for example, GS-DE, GS-PR, GS-TV and GS-LV for both the case of (Rk) and (Rpk).

With regard to (RSm), the main affecting parameter is tangential velocity (TV), followed by linear velocity (LV) and by grain size (GS). A low value of the grain size equal to 15 along with 40 m/min for the tangential velocity and 20 m/min for the linear velocity led to a value of (RSm) equal to 31.468 μm, and contrarily, a value of the grain size of 30 along with 20 m/min for the tangential velocity and 40 m/min for the linear velocity led to the maximum value of (RSm), which was 75.64 μm. Moreover, main interaction effects correspond to those related to (TV), like GS-TV, DE-TV, PR-TV and TV-LV.

Future research will include selecting different finishing conditions. On the other hand, different tools will be included.

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